

The Denoised, Deconvolved, and Decomposed *Fermi* γ -ray sky

An application of the D³PO algorithm

Marco Selig^{1,2}, Valentina Vacca¹, Niels Oppermann³, and Torsten A. Enßlin^{1,2}

¹ Max Planck Institut für Astrophysik (Karl-Schwarzschild-Straße 1, D-85748 Garching, Germany)

² Ludwig-Maximilians-Universität München (Geschwister-Scholl-Platz 1, D-80539 München, Germany)

³ Canadian Institute for Theoretical Astrophysics (60 St. George Street, Toronto, ON M5S 3H8, Canada)

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ABSTRACT

We analyze the 6.5 year all-sky data from the *Fermi* Large Area Telescope restricted to γ -ray photons with energies between 0.6–307.2 GeV. Raw count maps show a superposition of diffuse and point-like emission structures and are subject to shot noise and instrumental artifacts. Using the D³PO inference algorithm, we model the observed photon counts as the sum of a diffuse and a point-like photon flux, convolved with the instrumental beam and subject to Poissonian shot noise. The D³PO algorithm performs a Bayesian inference in this setting without the use of spatial or spectral templates; i.e., it removes the shot noise, deconvolves the instrumental response, and yields estimates for the two flux components separately. The non-parametric reconstruction uncovers the morphology of the diffuse photon flux up to several hundred GeV. We present an all-sky spectral index map for the diffuse component. We show that the diffuse γ -ray flux can be described phenomenologically by only two distinct components: a soft component, presumably dominated by hadronic processes, tracing the dense, cold interstellar medium and a hard component, presumably dominated by leptonic interactions, following the hot and dilute medium and outflows such as the *Fermi* bubbles. A comparison of the soft component with the Galactic dust emission indicates that the dust-to-soft-gamma ratio in the interstellar medium decreases with latitude. The spectrally hard component exists in a thick Galactic disk and tends to flow out of the Galaxy at some locations. Furthermore, we find the angular power spectrum of the diffuse flux to roughly follow a power law with an index of 2.47 on large scales, independent of energy. Our first catalog of source candidates includes 3,106 candidates of which we associate 1,381 (1,897) with known sources from the second (third) *Fermi* source catalog. We observe γ -ray emission in the direction of a few galaxy clusters hosting known radio halos.

Key words. methods: data analysis – methods: statistical – techniques: image processing – gamma-rays: general – gamma-rays: diffuse background – catalogs

1. Introduction

Since August 2008 the *Fermi* Gamma-ray Space Telescope has observed the γ -ray sky with its main instrument, the Large Area Telescope (LAT, Atwood et al. 2009), which is sensitive to photons with energies ranging from around 20 MeV to above 300 GeV.

There is a diversity of astrophysical contributions to the total γ -ray flux. Most of the photons in the GeV-range are induced by cosmic rays (CRs), charged particles moving at (ultra-)relativistic speeds, through hadronic interactions of CR nuclei with the interstellar medium (ISM) or inverse Compton scattering (IC) of electrons with background light (Ackermann et al. 2012d; Dermer et al. 2013). In addition, there is emission from an spatially constant diffuse background, which is commonly denoted as “extragalactic” background (Dermer 2007, and references therein), and from sources that appear point-like.

The diffuse and point-like γ -ray fluxes appear superimposed to an observer. An observation through an instrument, like the *Fermi* LAT for example, additionally convolves the total flux with the instrument response functions (IRFs). The gathered data are, lastly, subject to noise; i.e., Poissonian shot noise in the case of integer photon counts.

In order to retrieve the physical photon flux from observations, we would need to reverse those processes. Unfortunately, neither a direct inversion of the convolution nor the separation of noise and signal components is feasible exactly, so that we have to resort to alternative approaches.

One possibility is “forward” modeling, whereby parametrized models of different emission components are fit to the data; e.g., by a maximum-likelihood procedure as suggested by Ackermann et al. (2008) for the analysis of *Fermi* LAT data. By inspection of residuals between the data and the best fitting model(s), new features might be discovered. A famous example are the *Giant Fermi Bubbles* revealed by Su et al. (2010) using templates. Such templates are commonly constructed in accordance with surveys at lower energies or by modeling of the relevant CR physics (Ackermann et al. 2008; Su et al. 2010; Su & Finkbeiner 2012; Ackermann et al. 2012d, 2014c, and references therein).

In this work, we investigate the “backward” reconstruction of flux contributions using Bayesian inference methods (Bayes 1763; Cox 1946; Shannon 1948; Wiener 1949). The idea is to obtain signal estimates (and uncertainties) from an algorithm based on a probabilistic model that denoises, deconvolves, and decomposes the input data. This proba-

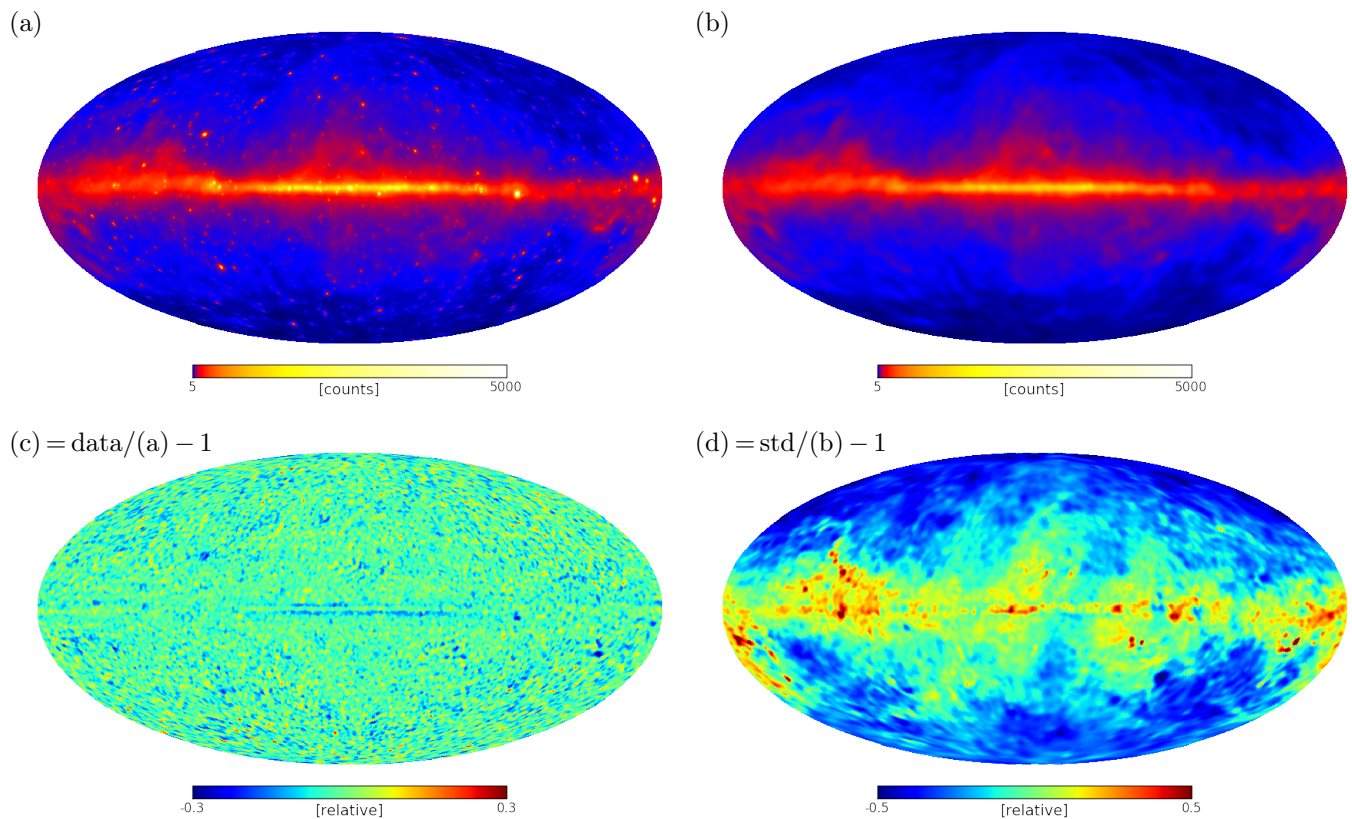


Fig. 1. Illustration of the γ -ray sky seen by the *Fermi* LAT in Mollweide projection. Panel (a) shows the (total) photon flux reconstructed from photon count data of 6.5 years mission elapsed time in the energy range from 0.6 to 307.2 GeV reconvolved with the LAT’s IRFs. Panel (b) shows solely the reconvolved diffuse contribution. Panel (c) shows the fractional residual map between data and reconstruction smoothed with a 0.5° Gaussian kernel. Panel (d) shows the fractional residual map between the standard Galactic diffuse model (short “std”) and the reconstructed diffuse contribution smoothed with a 0.75° Gaussian kernel.

bilistic model includes prior constraints to remedy the complexity of the inverse problem. Assuming a sparsity-based regularization, for example, Schmitt et al. (2010, 2012) proposed an analysis strategy using waveforms, which they applied to simulated *Fermi* data. For the analysis of X-ray images, which pose the same challenges as γ -ray images, a Bayesian background-source separation technique was proposed by Guglielmetti et al. (2009).

We deploy the D³PO inference algorithm (Selig & Enßlin 2013) derived within the framework of information field theory (IFT, Enßlin et al. 2009; Enßlin 2013, 2014). It simultaneously provides non-parametric estimates for the diffuse and the point-like photon flux given a photon count map. This challenging inverse problem is thereby regularized by prior assumptions that provide a statistical description of the morphologically different components; i.e., the priors define our naive understanding of “diffuse” and “point-like”. D³PO considers Poissonian shot noise, without Gaussian approximations, and takes the provided IRFs of the *Fermi* LAT fully into account. Furthermore, we can retrieve uncertainty information on the estimates.

All this allows us to present a continuous reconstruction of the diffuse γ -ray sky up to around 300 GeV, as well as an estimate of the point-like contribution, from which we derive the first D³PO *Fermi* catalog of γ -ray source candidates. By analyzing the spectral behavior of the diffuse component, it is possible to investigate the underlying pro-

cesses, especially with regard to the CRs responsible for the emission.

The remainder of this paper is structured as follows. Section 2 summarizes the analysis procedure, a more detailed description is given in Appendix A. We present and discuss our findings in Section 3, and conclude in Section 4.

2. Analysis summary

We analyze the photon count data collected by the *Fermi* LAT within its 6.5 years of operation. All data selection criteria, the working principle of the applied D³PO inference algorithm (Selig & Enßlin 2013), and a description of the analysis procedure are detailed in Appendix A.

In summary, we make use of the reprocessed Pass 7 available within the *Fermi* Science Tools¹ in order to retrieve the data, as well as the corresponding instrument response functions and exposure of the *Fermi* LAT (Atwood et al. 2009; Abdo et al. 2009; Ackermann et al. 2012a). We consider nine logarithmically spaced energy bands ranging from 0.6 to 307.2 GeV, cf. Table 1. For each band, we spatially bin all events classified as CLEAN in count maps, whereby we distinguish the front or back conversion of the photon within the LAT. Throughout this work, we discretize the sky using the HEALPIX scheme with

¹ <http://fermi.gsfc.nasa.gov/ssc/data/analysis/documentation/>

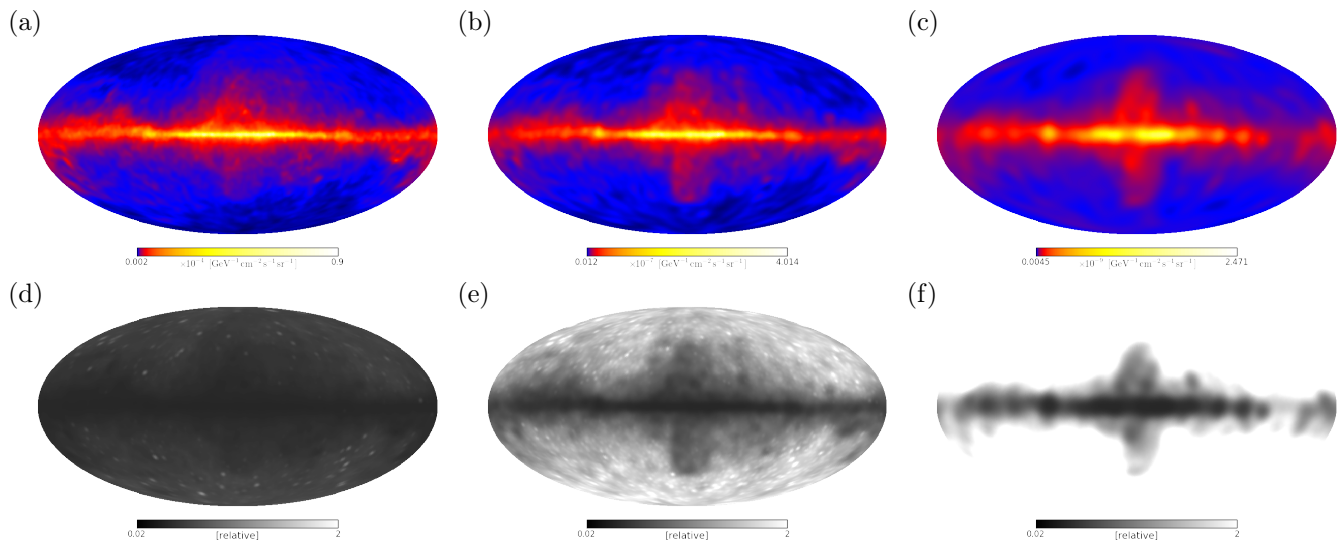


Fig. 2. Illustration of the diffuse γ -ray flux and its relative reconstruction uncertainty on a logarithmic scale at different energies in Mollweide projection. The panels (a–c) show the reconstructed diffuse photon flux at roughly 2 GeV, 10 GeV, and ~ 100 GeV. The photon flux is given in units of $\text{GeV}^{-1}\text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1}$. Notice that the color scale varies. The panels (d–f) show the relative uncertainty on the above reconstructions. Maps for all energy bands are contained in the online material.

$n_{\text{side}} = 128$, which corresponds to an angular resolution of approximately 0.46° .

This data set is the input for the D³PO algorithm. In order to denoise, deconvolve, and decompose the data, we suppose the data \mathbf{d} to be the result of a Poisson process with an expectation value given by the convolved sum of the diffuse and point-like flux, $\phi^{(s)}$ and $\phi^{(u)}$; i.e.,

$$\mathbf{d} \curvearrowright \mathcal{P}(\mathbf{d}|\mathbf{R}(\phi^{(s)} + \phi^{(u)})), \quad (1)$$

where the operator \mathbf{R} describes the full instrument response of the LAT. Under this model assumption, and with the aid of prior regularizations, D³PO computes estimates for the photon fluxes. The inference is performed iteratively until convergence and for each energy band separately. Further details regarding the inference can be found in Appendix A.

The results of this analysis – including, among others, the reconstructed fluxes, uncertainties, and the first D³PO *Fermi* (1DF) catalog of γ -ray source candidates – are publicly available at <http://www.mpa-garching.mpg.de/ift/fermi/>.

Table 1. Overview of the energy binning. Listed are minimum, logarithmic mean, and maximum energy for each bin.

band	E^{min} [GeV]	E^{mid} [GeV]	E^{max} [GeV]
1	0.60	0.85	1.20
2	1.20	1.70	2.40
3	2.40	3.40	4.80
4	4.80	6.79	9.60
5	9.60	13.58	19.20
6	19.20	27.15	38.40
7	38.40	54.31	76.80
8	76.80	108.61	153.60
9	153.60	217.22	307.20

3. Results and discussion

3.1. The γ -ray sky

The *Fermi* LAT has detected millions of γ -ray photons within the first 6.5 years of its mission. We can stack them in a binned all-sky count map disregarding the energy of the photons.

Figure 1 shows such all-sky maps for the total and the diffuse result of the reconstruction. D³PO denoises, deconvolves, and decomposes photon count maps yielding a reconstruction of the diffuse and point-like photon flux. A reconvolution of the reconstructed γ -ray flux with the instrument response functions demonstrates the quality of the performed denoising; i.e., the removal of Poissonian shot noise.

The fractional residual exhibits no significant structures and the mean of its absolute value is below 5%.² As we compare the data with a denoised reproduction, the major difference is due to shot noise. We observe a weak ringing around the Galactic plane, which is a numerical artifact due to imperfections of spherical harmonic transformations applied during the inference. Previous comparisons with best-fitting templates created by the GALPROP code (Moskalenko & Strong 2000; Strong et al. 2000; Ackermann et al. 2008, 2012d, and references therein) often show significant residuals indicating features lacked by the respective models; e.g., cf. Fig. 6 in Ackermann et al. (2012d). Since our inference machinery, on the contrary, is free of a *priori* assumption regarding the existence of any Galactic or extragalactic features, significant residuals are not to be expected.

² If we approximate the Poissonian $\mathcal{P}(\mathbf{d}|\boldsymbol{\lambda})$ by a Gaussian \mathcal{G} with mean $\boldsymbol{\lambda}$ and variance $\text{diag}[\boldsymbol{\lambda}]$, we can expect the mean of the absolute fractional residual to be

$$\frac{1}{N} \sum_{n=1}^N \frac{|d_n - \lambda_n|}{\lambda_n} \approx \frac{1}{N} \sum_{n=1}^N \frac{|\mathcal{G}(0,1)|}{\sqrt{\lambda_n}} \approx \frac{1}{N} \sum_{n=1}^N \sqrt{\frac{2}{\pi d_n}}.$$

For the considered data set, this computes to around 16%.

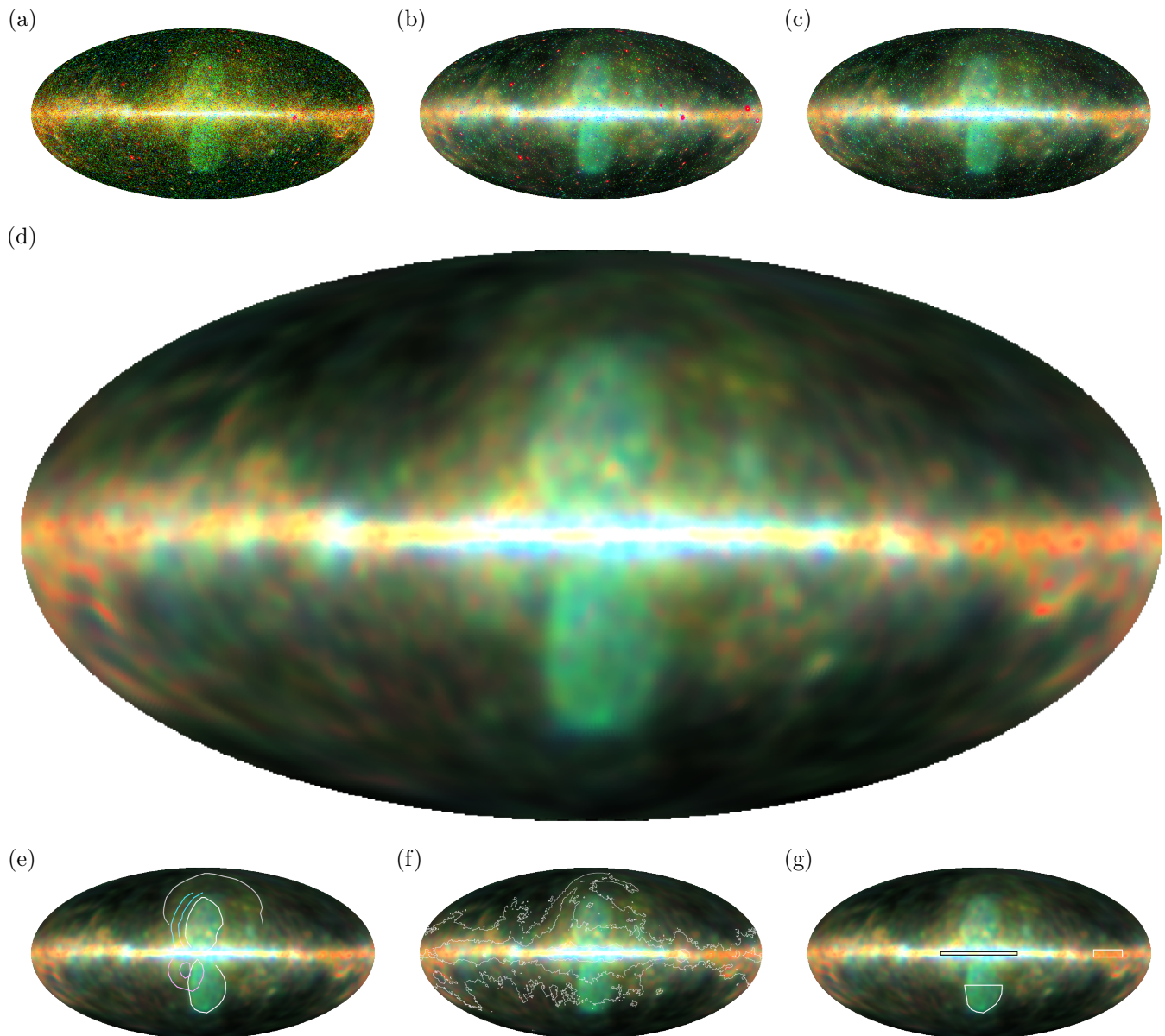


Fig. 3. Illustration of the γ -ray sky in pseudocolor in Mollweide projection. Panel (a) shows the 6.5 year data. The panels (b) and (c) show the reconstructed (total) photon flux that in (b) is reconvolved with the IRFs. Panel (d) shows the reconstructed diffuse photon flux. The panels (e) and (f) reproduce the latter but are overlaid with the feature contours found by Su et al. (2010) (white: *Giant Fermi Bubbles*, light magenta: *Donut*, light blue: *North Arc*, light gray: *Radio Loop I*) and contours of the 408 MHz radio map from Haslam et al. (1982), respectively. Panel (g) highlights the contours defining the “bulge”-, “cloud”-, and “bubble”-like regions discussed in Section 3.3.

Excluding the point-like contribution from the reconvolved count map, the diffuse γ -ray sky becomes fully revealed, see Fig. 1b. The diffuse count map clearly displays Galactic features and substructures within the ISM. In comparison to the standard Galactic diffuse model³, we find obvious residuals. These include diffuse structures on very small scales that are not captured in the reconstruction because its effective resolution is limited due to signal-to-noise and IRFs. At high latitudes, extragalactic contributions are reconstructed and yield an excess compared to the Galactic diffuse model. While the reconvolved photon count image appears somewhat smoothed, its deconvolved counterpart

³ The standard Galactic diffuse model is provided by http://fermi.gsfc.nasa.gov/ssc/data/analysis/software/aux/gll_iem_v05_rev1.fit.

displays the Milky Way in more detail. The diffuse γ -ray fluxes in the individual energy bands are shown in Fig. 2. The coarseness of the images increases with energy because the number of detected photons, and thus the signal-to-noise ratio, drops drastically. The uncertainties of the reconstructions are illustrated in the lower panels of Fig. 2. Nevertheless, the Galactic disk and bulge are clearly visible at all energies.

3.1.1. Pseudocolor images

In order to obtain a better view on the spectral characteristics of the γ -ray sky, we combine the maps at different energies by a pseudocolor scheme. This scheme is designed to mimic the human perception of optical light in the γ -

ray range. Intensity indicates the (logarithmic) brightness of the flux, and red colors correspond to low energy γ -rays around 1 GeV and blue colors to γ -rays up to 300 GeV. The resulting pseudocolor maps of the γ -ray sky are presented in Fig. 3. Thanks to a suitably tuned color response, spectrally different regions can easily be identified by the human eye. At a first glance, we can recognize the bright bulge of the Milky Way, the *Fermi* bubbles as two greenish blue, roundish areas, and red to yellowish cloud-like structures at low and intermediate latitudes, in particular around the Galactic anticenter.

The upper panels (a–d) illustrate the functionality of the D³PO inference algorithm showing the raw data and the denoised, deconvolved, and decomposed reconstruction, respectively. The denoising applies most strongly to the high energy bands, appearing green- to blueish, where the signal-to-noise ratios are worst. The deconvolution effect is most evident for point-like contributions in lower energy bands, appearing reddish, because of the increasing width of the point spread function (PSF) for these bands. Finally, the decomposition reveals the purely diffuse γ -ray sky.

This view reveals many interesting features beyond the Galactic disk and bulge, which we will discuss in the following.

3.1.2. Bubbles, features, and radio

The most striking features recovered by our reconstruction are the *Giant Fermi Bubbles* first found by Su et al. (2010). The bubbles extend up to $|b| \lesssim 50^\circ$ in latitude and $|l| \lesssim 20^\circ$ in longitude. They appear to emerge from the Galactic center, however, their astrophysical origin is still under discussion (Su et al. 2010; Crocker & Aharonian 2011; Cheng et al. 2011; Dogiel et al. 2011; Su & Finkbeiner 2012; Yang et al. 2014; Ackermann et al. 2014c, and references therein). In agreement with previous studies, we find the bubbles to have relatively sharp edges and an overall homogeneous surface brightness, appearing greenish blue in Fig. 3. Yang et al. (2014) report an energy dependent morphology of the southern bubble, which is, in particular, more extended to the Galactic South and West at high energies. Our results confirm this extension, as can be seen in the reconstruction for the highest energy band in Fig. 2.

Figure 3e also shows the *North Arc*, *Donut* and *Cocoon* (Su et al. 2010; Su & Finkbeiner 2012). However, we do not find evidence for a jet-like structure as reported by Su & Finkbeiner (2012).

Moreover, there is a correlation with structures seen at radio frequencies. For example, a comparison with the synchrotron map from Haslam et al. (1982) taken at 408 MHz reveals γ -ray counterparts of the *Radio Loop I* (Large et al. 1962) and smaller objects like the *Large Magellanic Cloud* at $(l, b) \approx (-80^\circ, -30^\circ)$, as well as the γ -ray glow around *Centaurus A* at $(l, b) \approx (-50^\circ, 20^\circ)$, see Fig. 3f. However, the resolution of the all-sky reconstruction is too coarse to detail the morphology of such small sources. A reconstruction of a more focused field of view would be necessary to that end.

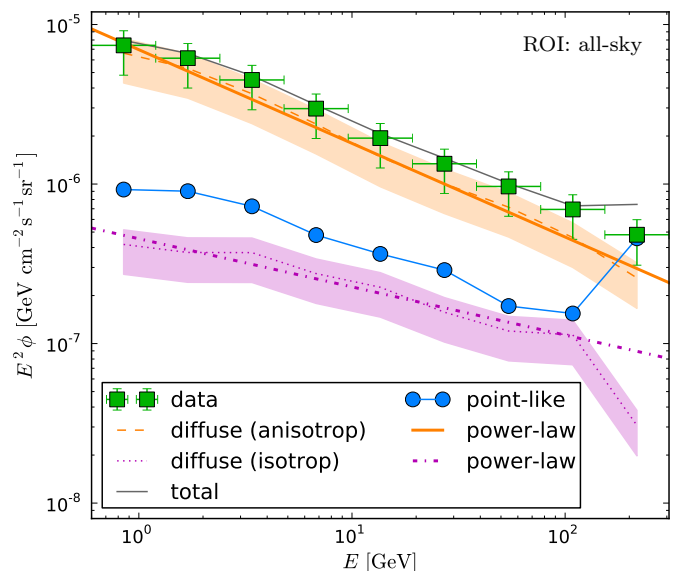


Fig. 4. Illustration of energy spectra considering an all-sky ROI. Shown are the data (green squares) converted to flux units, and spectra from the reconstructed total (gray), anisotropic diffuse (dashed orange), isotropic diffuse (dotted magenta), and point-like photon flux (blue circles). Furthermore, power-law fits for the anisotropic (thick solid orange) and isotropic emission (thick dash-dotted magenta) are shown. The errors include statistical and systematic uncertainties and are only shown for data and diffuse contributions for reasons of clarity.

3.2. Energy spectra and spectral indices

In order to get a more quantitative view on the different contributions to the γ -ray flux, we now investigate photon flux energy spectra.

Figure 4 shows the measured⁴ and reconstructed energy spectra for the whole sky. Further regions of interest (ROIs), which typically in- or exclude the Galactic center

⁴ The photon data \mathbf{d} can be converted into flux units by division by the respective exposure ε , solid angle Ω , and width of the energy band, according to

$$\phi_j = \phi(E_j^{\text{mid}}) \equiv \frac{1}{(E_j^{\text{max}} - E_j^{\text{min}})} \sum_{i \in \text{ROI}} \frac{1}{2\Omega_{\text{ROI}}} \left(\frac{d_{ij}^{\text{FRONT}}}{\varepsilon_{ij}^{\text{FRONT}}} + \frac{d_{ij}^{\text{BACK}}}{\varepsilon_{ij}^{\text{BACK}}} \right),$$

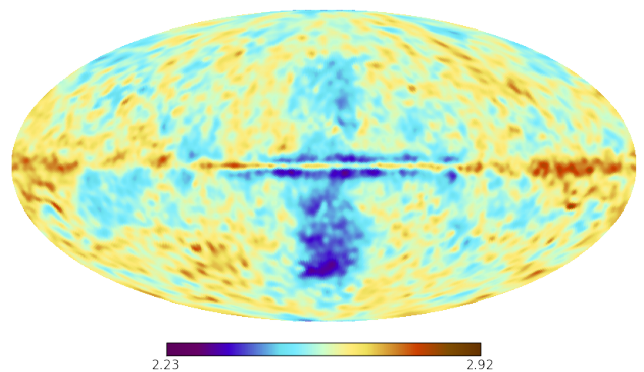


Fig. 5. Illustration of the spectral indices of featureless power-law fits, $\phi_{\text{aniso}} \propto E^{-\gamma}$, at all positions in the sky using energy bands 1–8.

or bulge, are investigated as well, see results in Table 2. The errors are dominated by systematics; i.e., by the uncertainty in the absolute energy scale $\Delta\mathcal{E}/\mathcal{E} = (+2\%, -5\%)$ (Ackermann et al. 2012c) and in the normalization of the effective area, which is $\pm 10\%$ up to 100 GeV and increases linearly with $\log(E)$ to $\pm 15\%$ at 1 TeV (Bregeon et al. 2013)⁵. The statistical uncertainties determined from the inference tend to track the signal-to-noise ratio.

We split the total energy spectrum into a diffuse and a point-like contribution, whereby we additionally distinguish between isotropic⁶ and anisotropic diffuse components. Overall, the spectra from the reconstructed fluxes agree well with the data, except for the highest energy bin, where the point-like component seems to be strongly overestimated. There are two reasons for this. On the one hand, the signal-to-noise ratio is lowest, and on the other hand, the PSF is sharpest. Therefore, the distinction between point-like sources, noise peaks, and weak diffuse emission breaks down. For this reason, we exclude this highest energy band from further spectral analysis.

The diffuse γ -ray flux amounts to $\sim 90\%$ of the total flux with the majority being anisotropic contributions of Galactic origin. Both diffuse contributions, isotropic and anisotropic, are consistent with featureless power laws, $\phi \propto E^{-\gamma}$. The results of the power-law fits are given in Table 2.

For the anisotropic component we find a spectral index $\gamma^{(s)} = 2.59 \pm 0.05$ that is slightly softer than the index of 2.44 ± 0.01 reported by Ackermann et al. (2012b) indicating a lack of flux at high energies, which can again be explained by the low signal-to-noise ratio in this regime. In low energy bands, the spectrum is dominated by the production and decay of π^0 -mesons induced by CR protons, while IC emission becomes increasingly important at the highest energies (Ackermann et al. 2012b,d). The declining tail of the pion bump, peaking at $\frac{1}{2}m_{\pi^0} \approx 0.07 \text{ GeV } c^{-2}$, is visible.

The isotropic background is often referred to as “extragalactic” because it comprises unresolved extragalactic sources and might include possible signatures from large-scale structure formation or dark matter decay (Dermer 2007; Abdo et al. 2010b, and references therein). The isotropic diffuse background also follows a featureless power law with a spectral index $\gamma_{\text{iso}}^{(s)} = 2.30 \pm 0.06$, if we ignore the last energy band. Notice that the excess of isotropic emission around $\sim 3 \text{ GeV}$ is rather insignificant with regard to the uncertainties.⁷ Abdo et al. (2010b) derive a spectral index of 2.41 ± 0.05 from 1 year *Fermi* LAT data in the energy range of 0.03–100 GeV. This indicates a slight spectral hardening of the isotropic background towards higher energies. In the same energy range, observations with the Energetic Gamma Ray Experiment Telescope (EGRET) yield a spectral index of 2.10 ± 0.03 that is considerably smaller (Sreekumar et al. 1998). This discrepancy, which might be an instrumental issue, is not yet clarified.

where the indices i and j label pixels and energy bands, respectively. Notice that front- and back- converted data are averaged accordingly.

⁵ See also http://fermi.gsfc.nasa.gov/ssc/data/analysis/LAT_caveats.html.

⁶ In this context, “isotropic” means spatially constant.

⁷ Such a tentative excess could be a line-like signal from dark matter decay/annihilation (Conrad 2012), however, this is highly speculative considering the available data.

The recent analysis by Ackermann et al. (2014b) investigating an energy range of 0.1–820 GeV reports the isotropic γ -ray background to be consistent with a power law with exponential cut-off at 280 GeV having a spectral index of 2.32 ± 0.02 . This is consistent with our findings.

If we consider smaller ROIs, we find fluctuations in the spectral index of the diffuse γ -ray flux. These fluctuations could give some indication about the CR spectrum, the composition of the local ISM, etc.

Since the D³PO algorithm provides a continuous estimate of the diffuse photon flux, we can perform a spectral analysis in individual pixels. Although the energy spectra vary with location, we, for simplicity, assume a general power-law behavior everywhere, but with varying spectral index. Figure 5 shows the obtained spectral index map for the anisotropic γ -ray sky, centered on the average index of 2.6. The spatial smoothness of the spectral index map reflects that there are no discontinuities between neighboring pixels in the reconstructions.

From this spectral index map it is apparent that the Galactic disk is spectrally softer than the all-sky average. The same holds for the extensive structures that trace interstellar gas. These regions are dominated by hadronic interactions releasing γ -ray photons; e.g. π^0 production and decay (cf. e.g., Ackermann et al. 2012d).

In the region overlapping with the *Giant Fermi Bubbles* we find overall similar spectra that are, however, harder than the all-sky average. This is in agreement with the results of Ackermann et al. (2014c), although they found a log-parabola to fit best. The strong hardening towards the high latitude edge of the southern bubble comes from its increased spatial extent compared to lower energies, cf. Yang et al. (2014). Further local spots inside the bubble region are insignificant within the statistical and systematic uncertainties.

Although the morphology and spectra of the bubbles can be explained with hadronic and leptonic CR processes, IC scenarios give the preference of also reproducing the microwave haze observed with WMAP and *Planck* (Planck Collaboration 2013b; Yang et al. 2013; Ackermann et al. 2014c). Furthermore, the low target densities at higher Galactic latitudes render the hadronic scenario as not very compelling.

3.3. Diffuse emission components

The pseudocolor scheme introduced in Section 3.1.1 already allows us to visually inspect the continuous reconstruction of the diffuse γ -ray sky. By eye, we can make out the Galactic bulge, the *Fermi* bubbles, and also cloudy structures around the Galactic anticenter.

In order to confirm this impression the visualization gives, we retrieve energy spectra from three characteristic regions: “bulge”-like ($|l| < 40^\circ, |b| < 1.5^\circ$), “cloud”-like ($-150^\circ < l < -120^\circ, |b| < 3^\circ$), and “bubble”-like (for which we select the southern bubble up to latitudes $b < -27.5^\circ$). The contours of those regions are shown in Fig. 3g.

Figure 6a shows the energy spectra retrieved from the three regions. The “cloud”-like spectrum is rather soft ($\gamma^{(s)} \approx 2.6$) and features the tail of the pion bump. It is not surprising that the “cloud”-like spectrum is dominated by emission from π^0 decay, because the cloudy structures trace the gas content of the ISM that provides the target protons for π^0 production. The “bubble”-like spectrum is

Table 2. Overview of the ROIs. Listed are inclusion cuts in Galactic longitude l and latitude b , covered solid angle Ω , fitted spectral indices $\gamma^{(s)}$, and χ^2 divided by the degrees of freedom (DOF); i.e., 9 bands–2 unknowns = 7. The latter two are given for the anisotropic and the isotropic diffuse photon flux, respectively.

ROI	inclusion cuts	Ω [sr]	$\gamma^{(s)}$	χ^2/DOF	$\gamma_{\text{iso}}^{(s)}$	$\chi_{\text{iso}}^2/\text{DOF}$
1	all-sky	4π	2.59 ± 0.05	0.10	2.30 ± 0.06	0.14
2	$ b > 10^\circ \vee l < 10^\circ$	10.5	2.60 ± 0.05	0.22	2.30 ± 0.06	0.14
3	$ b > 10^\circ$	10.4	2.63 ± 0.05	0.39	2.30 ± 0.06	0.14
4	$ b < 10^\circ \wedge l < 80^\circ$	4.5	2.52 ± 0.05	0.08	2.52 ± 0.06	0.06

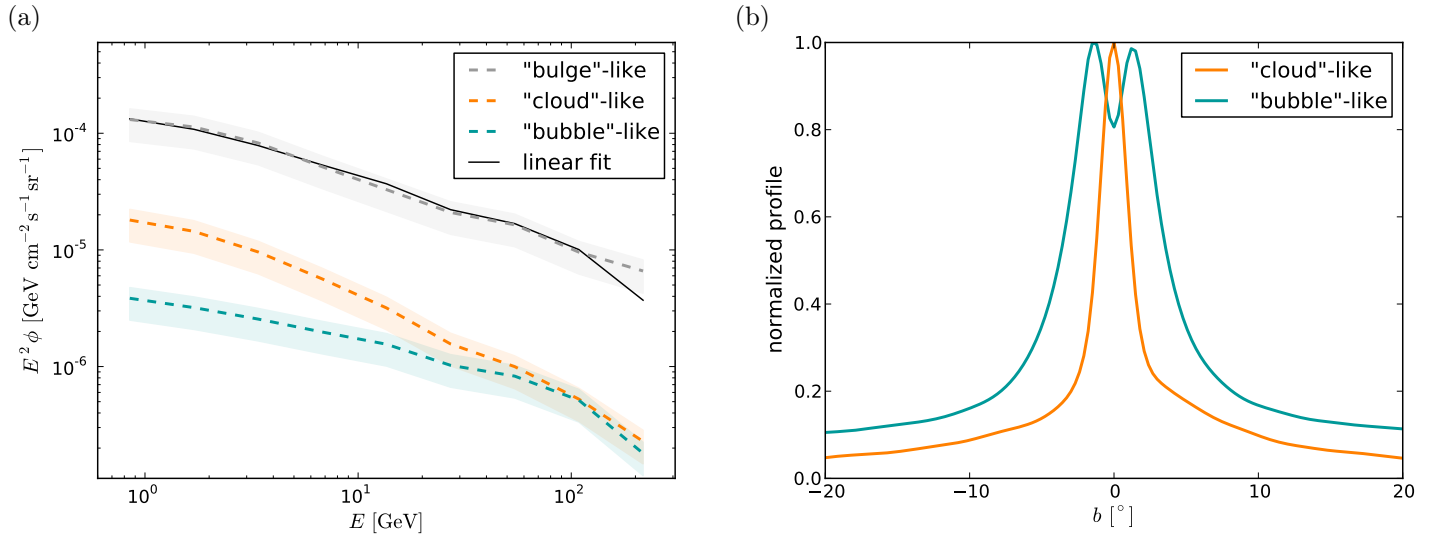


Fig. 6. Illustration of “cloud”-, and “bubble”-like component. Panel (a) shows energy spectra from ROIs defined in Fig. 3g, cf. text. In addition to the spectra retrieved from the different regions, a linear combination of the “cloud”-, and “bubble”-like is fit to the “bulge”-like component, cf. legend. Panel (b) shows the normalized latitude profiles of the “cloud”-, and “bubble”-like component.

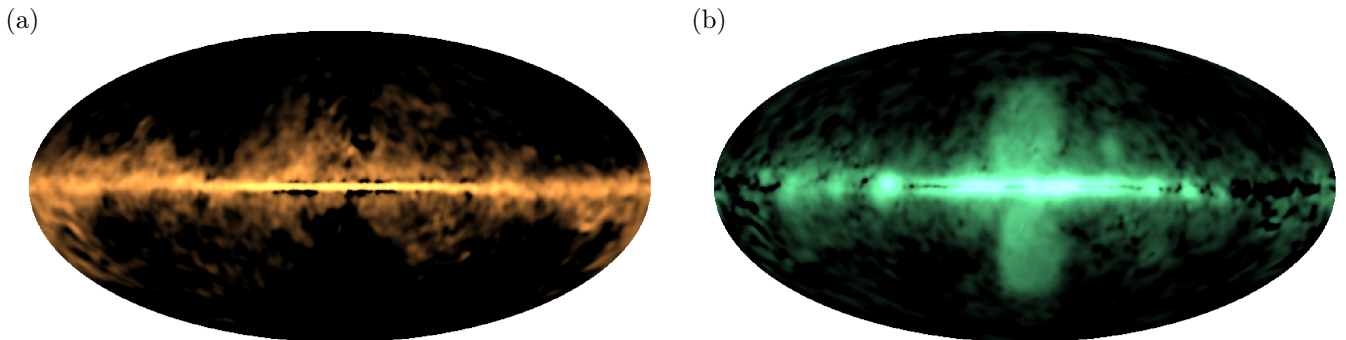


Fig. 7. Illustration of the γ -ray sky in pseudocolor in Mollweide projection. Panel (a) shows the “cloud”-like diffuse component and panel (b) the “bubble”-like one.

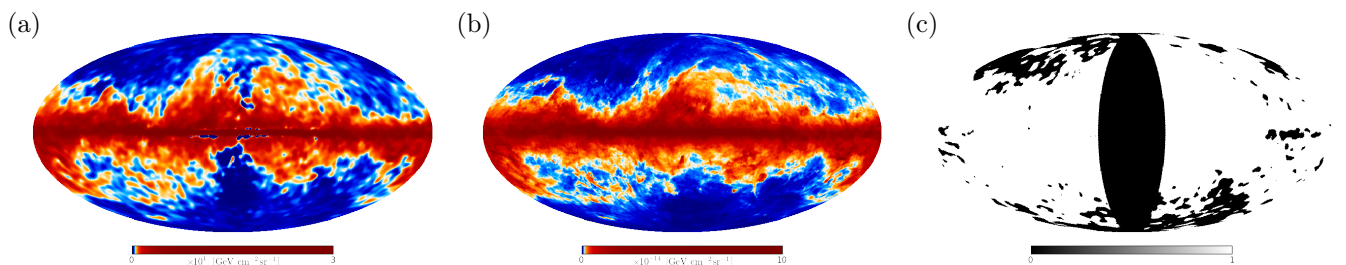


Fig. 8. Illustration of the brightness in Mollweide view. Panel (a) shows the integrated brightness of the “cloud”-like component. Panel (b) shows the monochromatic brightness of thermal dust emission at 353 GHz (Planck Collaboration 2013a). Panel (c) shows in white the area included in computing the latitude profile in Fig. 9.

significantly harder ($\gamma^{(s)} \approx 2.4$) indicating the dominance of hard processes like IC emission. The “bulge”-like region

exhibits a spectrum that, besides having a higher absolute scale, can be described as a linear combination of the former two spectra, cf. Fig. 6a.

As the “bulge”-like spectrum is found to be a linear combination of “cloud”- and “bubble”-like, we can try to decompose the whole diffuse sky into those two components. For this purpose, we fit the spectrum in individual pixels by the “cloud”-, and “bubble”-like component.⁸ The fit coefficients then indicate the strength of the “cloud”- or “bubble”-like contribution at all locations. Multiplying the fit coefficients with the respective spectra, we obtain a pseudocolor visualization of the “cloud”- or “bubble”-like emission components as shown in Fig. 7.

In spite of the simplicity of this two-component model, we find a good agreement between the total diffuse emission and the sum of the two components. The relative residuals are around 5–13%, except for the highest energy band, which was excluded from the fitting procedure, where the error is approximately 28%. Our findings demonstrate that the γ -ray sky in the energy range from 0.6 to 307.2 GeV can

⁸ In case the fit suggests a negative coefficient for one component, the fitting procedure is repeated ignoring this component. In this way, we ensure the positivity of the components.

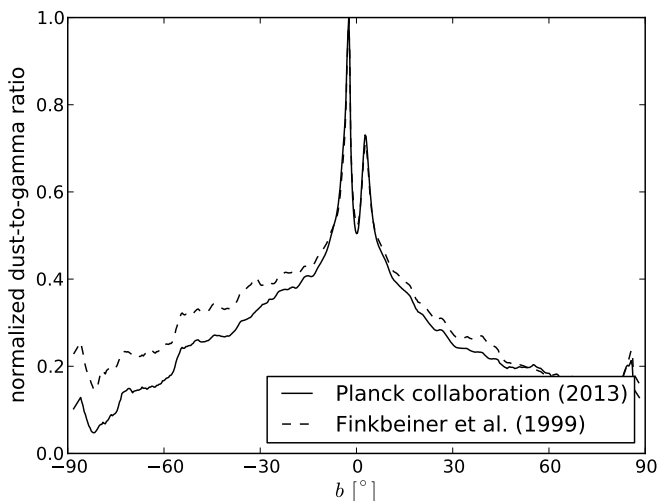


Fig. 9. Illustration of the latitude profile of the dust-to-“cloud”-like-gamma ratio. The thermal dust emission from Planck Collaboration (2013a), and Finkbeiner et al. (1999) has been smoothed with a 0.7° Gaussian kernel to match the coarseness of the γ -ray map.

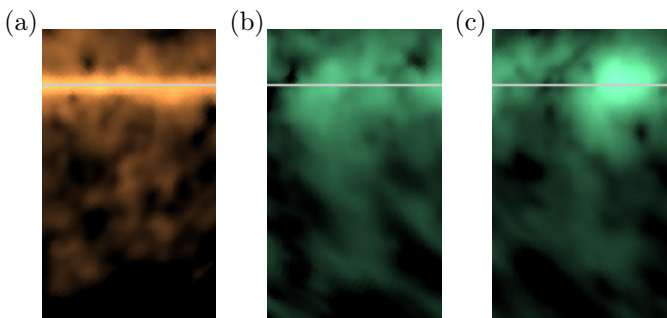


Fig. 10. Panel (a) shows a magnification of the *Chamaeleon* complex from Fig. 7a. Panel (b) and (c) show magnifications of tentative outflows from Fig. 7b. The light gray line marks the Galactic plane ($l = 0^\circ$).

with high precision be described by “cloud”- and “bubble”-like emission components only.

From the shape of the energy spectrum of the “cloud”-like component, we deduced that it is dominated by hadronic processes. We can also compare its morphology with other ISM tracers. For this, we compute the brightness of the “cloud”-like component and show it in Fig. 8a. The resulting map agrees with the thermal dust emission seen by *Planck* (Planck Collaboration 2013a) at 353 GHz shown in Fig. 8b. We like to stress how similar the morphology of thermal dust microwave/IR emission and the “cloud”-like γ -ray component are. In particular in the cloudy region in the Galactic East, the structures agree well, although we took the spectrum from a region in the West. As the thermal dust emission traces the densest part of the ISM, and hence the target gas for the CR protons, we are confident that the “cloud”-like component is indeed dominated by hadronic emission processes.

The *Chamaeleon* complex, around $(l, b) \sim (-60^\circ, -20^\circ)$, hosting a number of star-forming clouds is visible in the “cloud”-like component, cf. Fig. 10a. Recent work by the Planck Collaboration (2014) used γ -, radio-, and dust data to map the local gas content of the clouds.

The “cloud”-like component is, however, morphologically not exactly identical to the dust emission. For example, in the latitude profile shown in Fig. 9, the dust-to-gamma ratio decreases with increasing latitude. This profile was computed including only pixels outside the bubble region ($|l| > 30^\circ$), where both, the “cloud”- and “bubble”-like component, contribute, and the estimated *Planck* dust emission is positive. The dust seems to be preferentially in the Galactic disk compared to the thermal gas traced by γ -rays. The morphology of the “bubble”-like component is very different, cf. Fig. 7. Since the spectrum of the *Fermi* bubbles is spatially relatively constant, the shape of the northern bubble is well recovered based on the spectrum of the southern one. We also find an excess in the “bubble”-like emission in the bulge region (de Boer & Weber 2014), as well as in the star forming region *Cygnus-X* around $(l, b) \sim (80^\circ, 0^\circ)$. Excess of emission following the “bubble”-like spectrum is also visible at intermediate latitudes exhibiting mushroom-like shapes typical for hot outflows; e.g., South of the *Cygnus-X* region ($(l, b) \sim (90^\circ, < -15^\circ)$), or along $(l, b) \sim (130^\circ, < -15^\circ)$, cf. Fig. 10b and c. Those are likely candidates for outflows from active star-forming regions of the Milky Way. Furthermore, the latitude profile shown in Fig. 6b indicates that the “bubble”-like disk is roughly twice as thick as the “cloud”-like component.

Since the “bubble”-like γ -ray emission is morphologically so distinct, and sets itself apart from the “cloud”-like component, we suppose that the two components are dominated by different emission processes. The “bubble”-like spectrum is distinctly harder and less structured, therefore a leptonic emission process, in particular IC scattering, seems more convincing in causing the “bubble”-like diffuse component.

The CR populations producing these two γ -ray emission components do not need not to be very different. It might be that we are just seeing two different phases of the ISM:

- the cold and condensed phase carries most of the Galactic dust and has a sufficient nuclei target density to be predominately revealed through hadronic interactions with CR protons. Hence, the resulting γ -ray emission mostly traces the highly structured gas distribution.

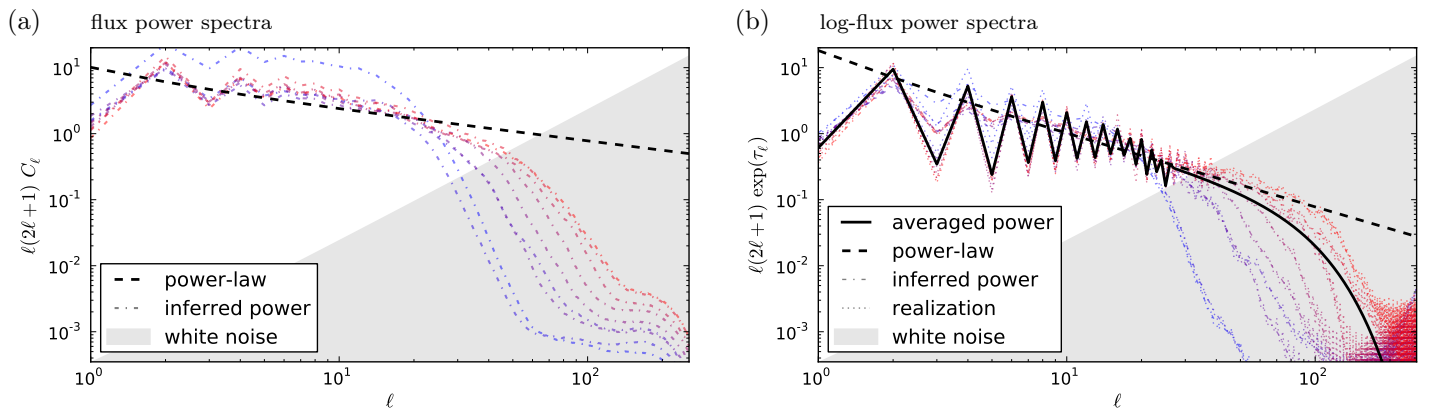


Fig. 11. Illustration of angular power spectra over angular quantum number ℓ . Panel (a) shows the inferred spectra of the diffuse photon flux $\phi^{(s)}$ in each energy band and a power-law fit thereof, cf. legend. Panel (b) shows the direct realization spectra of the diffuse signal $s = \log(\phi^{(s)}/\phi_0)$, as well as the inferred, fitted, and averaged spectra, cf. legend. The colors (from red over violet to blue) indicate energy (from band 1 to 9) in both panels and a white noise spectrum with arbitrary normalization is included for comparison.

- the hot, dilute, and voluminous phase tends to flow out of the Galactic disk. The γ -ray emission from within is dominated by IC upscattering of the Galactic photon field by CR electrons. As the photon field is relatively homogeneous, the morphology of the “bubble”-like component is probably shaped by the spatial distribution of the CRs.

This simple two-component model of the diffuse γ -ray emission supports scenarios in which the *Fermi* bubbles are just outflows of the hot ISM (Yang et al. 2013; Cheng et al. 2011; Dogiel et al. 2011; Chernyshov 2011; Carretti et al. 2013).

3.4. Angular power spectra

Under the assumption of statistical isotropy and homogeneity the second moments of a diffuse signal field are defined by its angular power spectrum. Studying power spectra gives some indication of the strength of typical fluctuations on respective angular scales described by the angular quantum number ℓ . According to our chosen HEALPIX discretization, we examine spectra up to a maximum scale set by $\ell_{\max} = 2n_{\text{side}} = 256$.

Figure 11 shows the angular power spectra of the diffuse photon flux $\phi^{(s)}$ – the quantity we are interested in – and its logarithm, the diffuse signal field s . The power spectrum, which is *a priori* unknown, needs to be reconstructed from the data alongside the diffuse signal field (Wandelt et al. 2004; Jasche et al. 2010; Enßlin & Frommert 2011; Oppermann et al. 2012; Jasche & Wandelt 2013). This is done for each energy band separately. Further details on the inference procedure can be found in Appendix A.

The inferred power spectra of s show similar power-law behavior at all energies with some remarkable deviations. On large scales, $0 < \ell \lesssim 28$, the spectra exhibit a strong distinction between even and odd ℓ -modes. The reason for this is the dominant contribution of the Galactic disk centered around $b = 0^\circ$ to the diffuse photon flux, which excites/suppresses even/odd ℓ -modes in the reconstruction. On smaller scales, on the other hand, the power spectra start to fall off because small-scale features cannot be resolved due to the finite exposure of the *Fermi* LAT. This effect has a clear energy dependence. Since events with higher energies are rarer, the decline of spectra from high-

energy bands begins at lower ℓ . Notice that the threshold set by the PSF is on very small scales; e.g., the 68% angular containment radius above 10 GeV is smaller than 0.2° corresponding to $\ell \gtrsim 900$.

Let us now consider the actual angular power spectrum C_ℓ of the diffuse photon flux $\phi^{(s)} \propto \exp(s)$. This can be computed by transforming⁹ the inferred (final) power spectra of s according to Greiner & Enßlin (2013). This transformation shifts power between different ℓ -modes, in particular toward smaller scales (larger ℓ). Again, we find a power-law behavior of the angular power spectrum, as can be seen in Fig. 11a. We fit a power-law with index $\gamma_\ell^{(s)} = 2.47 \pm 0.02$. There is an energy-dependent break point, though, beyond which the power drops. The break point should shift to higher ℓ with increasing observation time.

3.5. Point sources

Another result of our analysis of the 6.5 year *Fermi* data is a reconstruction of the point-like contribution to the photon flux, $\phi^{(u)}$, which consists of Galactic and extragalactic point sources.

Figure 12 shows an all-sky map of all point source candidates in the pseudocolor scheme introduced in Sec. 3.1.1. Markers (and their opacity) in the map indicate the position (and detection significance) of point sources from the second *Fermi* LAT source catalog (Nolan et al. 2012).¹⁰ There is a diversity of sources, which is why we highlight a selection by special markers. The brightest γ -ray sources are pulsars (PSRs) like *Vela* (PSR J0835-4510), *Geminga* (PSR J0633+1746), and *Crab* (PSR J0534+2200), but there are also pulsars that have first been detected in γ -ray; e.g., LAT PSR J0007+7303 and LAT PSR J0357+3205. The Galactic disk, and especially the bulge, is clustered with point sources including, among others, supernova remnants

⁹ Here, we disregard the respective monopole (mode with $\ell = 0$) for convenience. As a consequence, the absolute scale of the power spectrum of the diffuse γ -ray flux $\phi^{(s)}$ becomes ambiguous.

¹⁰ For further details regarding the *Fermi* LAT source catalog see http://fermi.gsfc.nasa.gov/ssc/data/access/lat/2yr_catalog/.

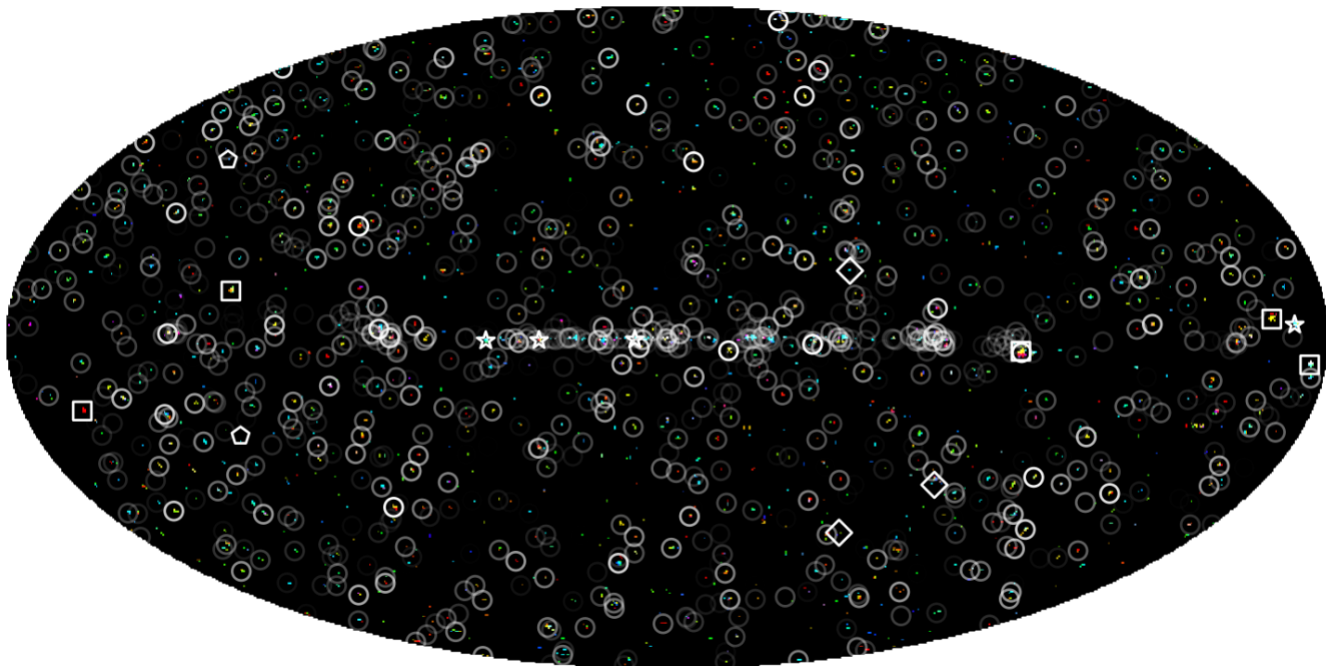


Fig. 12. Illustration of the point sources in the γ -ray sky in pseudocolor and in Mollweide projection. Markers show point sources from the second *Fermi* LAT source catalog (Nolan et al. 2012) for comparison, whereby the gray scale indicates their average detection significance as listed in the catalog. Special markers show a selection of pulsars (squares), local SNRs (stars), and well-known galaxies (pentagons), as well as famous extragalactic objects (diamonds), cf. text.

(SNRs) like W51C, W44, W30, and IC443. There are also many homogeneously distributed extragalactic sources, for example, the starburst galaxy *Cigar* (M82) or our neighboring galaxy *Andromeda* (M31). Furthermore, the core of *Centaurus A* (NGC 5128) and the *Small* and *Large Magellanic Cloud* are visible in γ -rays.

Deriving a catalog of source candidates from the point-like flux is difficult because a point source might, for example, appear in neighboring pixels at different energies due to different noise realizations and the aforementioned energy dependence of the signal-to-noise ratio and the PSF. In order to nominate a candidate, we check if the point-like contribution exceeds 2σ above the diffuse emission in at least two of the energy bands 1–8, which is a simple but conservative criterion taking the diffuse reconstruction uncertainty σ into account, cf. Fig. 2. Notice that we exclude the highest energy band from our search, since the point-like flux in this band seems to be contaminated as discussed in Sec. 3.2. We refer to the compiled point source catalog as the first D³PO *Fermi* (1DF) catalog of γ -ray source candidates.

Qualitatively, the point-like flux found by D³PO agrees with the second *Fermi* LAT source catalog as shown in Fig. 12. A few sources appear slightly off-center or smeared out over two or more pixels. The reason for this is that such sources are positioned between grid points of the chosen HEALPIX grid. Notice that image pixels in Fig. 12 do not represent HEALPIX pixels.

We find **3,106** source candidates, cf. Table 3. For comparison, the 1, 2, and 4 year *Fermi* LAT source catalogs comprise 1,451, 1,873, and 3,034 sources, respectively (Abdo et al. 2010a; Nolan et al. 2012; The Fermi-LAT Col-

laboration 2015). 1,381 (1,897) of our sources can be associated with known LAT sources from the second (third) catalog as the angular distance between 1DF candidate and catalog source is less than the angular resolution of our reconstruction. The reason why we do not confirm all objects in the second (third) *Fermi* LAT source catalog is the conservative criterion we apply. This still leaves 1,253 (1,209) new source candidates to be confirmed by future work.

We caution that a more detailed study is necessary to confirm or reject those candidates. The analysis of the individual sources, best done on more constrained ROIs and with higher angular resolution, is left for future work.

The present catalog includes extended objects as, e.g., SNRs. In the second *Fermi* LAT catalog 6 firm identifications, 4 associations, and 58 possible associations with SNRs are given. We detect more than 55% of them. In particular, 5 out of their 6 firm identifications are listed as 1DF candidates. For SNRs with fluxes $F \gtrsim 10^{-8} \text{ cm}^{-2} \text{ s}^{-1}$, our results are in good agreement with those of the *Fermi* collaboration. On the other hand, for faint sources we often recover smaller fluxes indicating the missing flux might be attributed to the diffuse emission. For a few sources we estimate a larger flux than given in the *Fermi* LAT catalog. For example, we measure $1.25 \times 10^{-7} \text{ cm}^{-2} \text{ s}^{-1}$ for SNR W44 in comparison to $7.96 \times 10^{-8} \text{ cm}^{-2} \text{ s}^{-1}$ in the *Fermi* LAT catalog. To overcome this issue, a modeling that takes into account the presence of discrete extended sources would be required, which is left for future work.

In the following, we compare the 1DF candidates for which we find a unique association within the second *Fermi* LAT source catalog (Nolan et al. 2012) by means of their spectral index and total flux. Notice that the two studies are

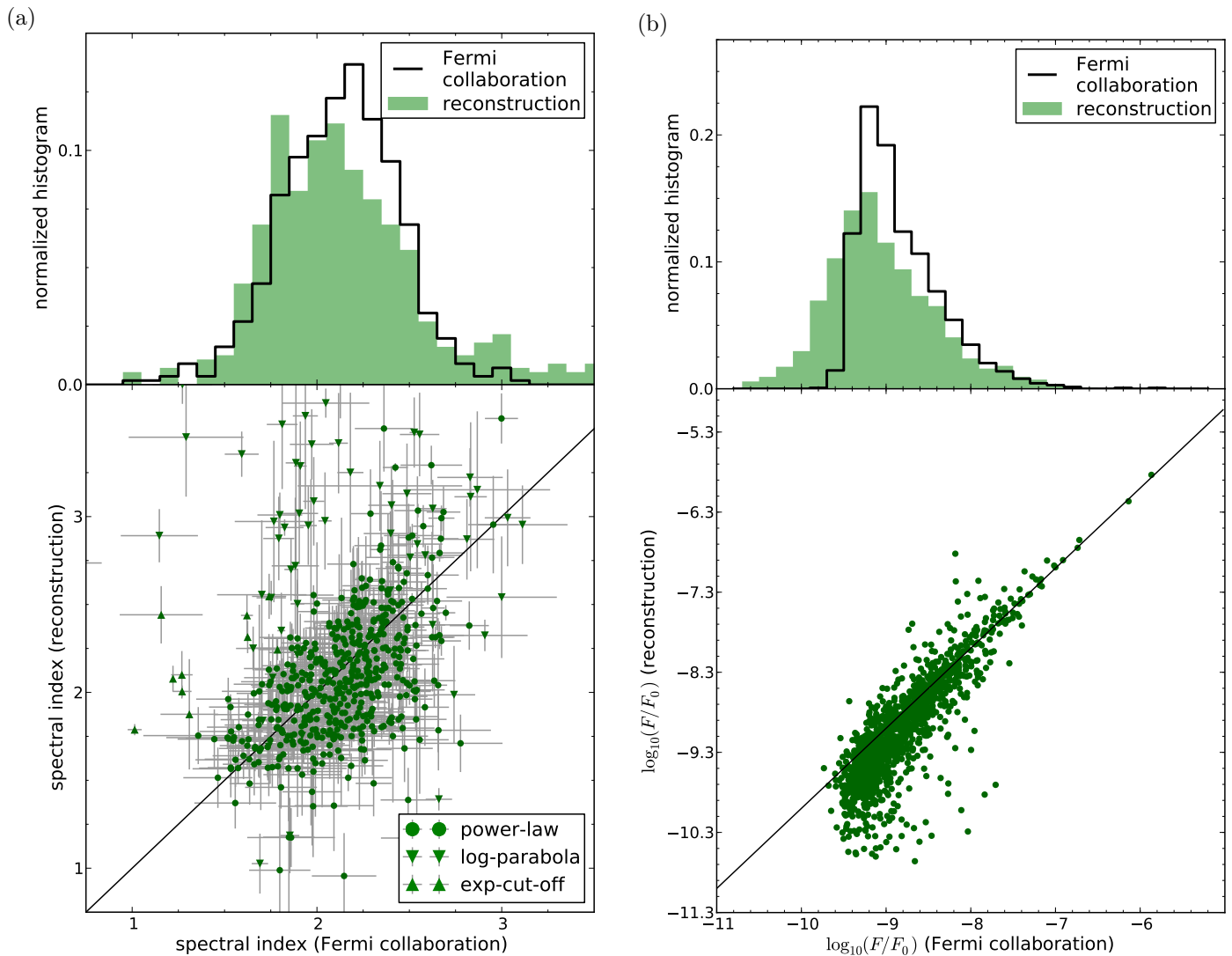


Fig. 13. Comparison of the second *Fermi* LAT source catalog (Nolan et al. 2012) and candidates from the reconstruction for which an association in the second *Fermi* LAT catalog has been found. Panel (a) shows the histogram and scatter plot of the spectral indices $\gamma^{(u)}$ of candidates versus catalog sources. In the latter, a 1 : 1 line (black solid) is plotted for comparison, and the markers indicate the fit spectral shape, cf. legend. Panel (b) shows the histogram and scatter plot of the logarithmic total fluxes $\log_{10}(F/F_0)$, where $F_0 = 1 \text{ cm}^{-2} \text{ s}^{-1}$. The scatter plot contains a 1 : 1 line (black solid) for comparison.

Table 3. Extract from the 1DF catalog. Listed are candidate ID (derived from the HEALPIX index), position in Galactic longitude l and latitude b , total flux between 1–100 GeV, contributing energy bands, and distance to the associated source in the second *Fermi* LAT source catalog (Nolan et al. 2012). The full catalog including uncertainties and associations with the third *Fermi* LAT source catalog is available online at <http://www.mpa-garching.mpg.de/ift/fermi/> as a FITS table.

candidate ID	l [°]	b [°]	$F^{(u)}$ [$\text{cm}^{-2} \text{ s}^{-1}$]	contributing energy bands	dist. [°]	primary association	...
1DF103542	263.5	-2.8	1.5×10^{-6}	✓✓✓✓✓✓✓✓✓✓	0.09	2FGL J0835.3–4510	...
1DF091157	195.2	4.3	6.9×10^{-7}	✓✓✓✓✓✓✓✓✓✓	0.12	2FGL J0633.9+1746	
1DF009247	179.9	65.0	4.1×10^{-8}	✓✓✓✓✓✓✓✓✓✓	0.08	2FGL J1104.4+3812	
1DF108550	184.6	-5.7	1.8×10^{-7}	✓✓✓✓✓✓✓✓✓✓	0.06	2FGL J0534.5+2201	
1DF036698	63.6	38.9	1.2×10^{-8}	✓✓✓✓✓✓✓✓✓✓	0.08	2FGL J1653.9+3945	
1DF159099	86.1	-38.3	1.1×10^{-7}	✓✓✓✓✓✓✓✓✓✓	0.12	2FGL J2253.9+1609	
1DF056702	88.9	25.0	1.0×10^{-7}	✓✓✓✓✓✓✓✓✓✓	0.07	2FGL J1836.2+5926	
1DF029553	21.9	43.9	1.4×10^{-8}	✓✓✓✓✓✓✓✓✓✓	0.04	2FGL J1555.7+1111	
1DF080298	119.8	10.5	6.9×10^{-8}	✓✓✓✓✓✓✓✓✓✓	0.17	2FGL J0007.0+7303	
1DF176024	17.9	-52.4	2.3×10^{-8}	✓✓✓✓✓✓✓✓✓✓	0.18	2FGL J2158.8–3013	
⋮							⋮

based on different data, exposure, calibration, and analysis algorithms.¹¹

P7_V6 (P7REP_V15) IRFs in the second *Fermi* LAT source catalog (Nolan et al. 2012) (the candidate catalog presented here).

¹¹ The main differences are the selection of SOURCE (CLEAN) events, the 2 (6.5) years of observation, and the usage of the

The spectral index of a source should not (or at least not strongly) be influenced by those differences. For each source, we attempt to fit three different spectral shapes: a plain power-law,

$$\phi^{(u)}(E) = K \left(\frac{E}{E_0} \right)^{-\gamma^{(u)}}, \quad (2)$$

a log-parabola,

$$\phi^{(u)}(E) = K \left(\frac{E}{E_0} \right)^{-\gamma^{(u)} - \beta \log(E/E_0)}, \quad (3)$$

and a power-law with exponential cut-off,

$$\phi^{(u)}(E) = K \left(\frac{E}{E_0} \right)^{-\gamma^{(u)}} \exp\left(-\frac{E - E_0}{E_{\text{cut}}}\right). \quad (4)$$

Here $E_0 = 1 \text{ GeV}$ serves as a reference energy, and the spectral index $\gamma^{(u)}$ is a fit parameter as are K , β , and E_{cut} . The 1DF source catalog contains the best-fit parameters for all shapes if applicable.

Figure 13a shows the comparison of the 1DF spectral indices and the ones listed in the second *Fermi* LAT source catalog (corrected to E_0 where needed). The scatter of spectral indices is large, but comparable to the uncertainties. We find a rough agreement, although our distribution is broadened toward higher indices. Most of the outliers yielding a high (low) spectral index are modeled by a log-parabola (exponential cut-off) that has an additional degree of freedom compared to the plain power law. This implies that the versatility of point source spectra might not be covered by the considered spectral shapes.

Figure 13b shows a comparison of the total fluxes $F^{(u)}$, defined as

$$F^{(u)} = \int d\Omega \sum_{j=1}^8 \int_{\tilde{E}_j^{\text{min}}}^{\tilde{E}_j^{\text{max}}} dE \left(\frac{E}{E_j^{\text{mid}}} \right)^{-\gamma^{(u)}} \phi^{(u)}(E_j^{\text{mid}}) \quad (5)$$

with j labeling the energy bands and

$$\begin{aligned} \tilde{E}_j^{\text{max}} &= \min\{1 \text{ GeV}, E_j^{\text{min}}\} \\ \tilde{E}_j^{\text{min}} &= \max\{E_j^{\text{max}}, 100 \text{ GeV}\}, \end{aligned}$$

in a histogram and a scatter plot. The fluxes show a good overall agreement. At the faint end, our fluxes tend to come below the fluxes reported in the second *Fermi* LAT source catalog (Nolan et al. 2012). Since our analysis benefits from a higher exposure and improved calibration, the fluxes from the *Fermi* collaboration might rather be considered as upper limits in this comparison.

3.5.1. Galaxy clusters

Some galaxy clusters exhibit diffuse, extended radio emission, so-called radio halos, which proves the existence of relativistic electrons therein. If relativistic protons are present as well, γ -ray emission is to be expected due to hadronic interactions (Ackermann et al. 2010, 2014a, and references therein).

Feretti et al. (2012) provide a collection of clusters hosting radio halos. We investigate the presence of γ -ray emission in the direction of those clusters and in the direction

of the clusters listed by Ackermann et al. (2010, 2014a), which would in our reconstruction appear point-like due to the pixelization of our reconstruction. Table 4 lists our upper limits on the total flux F^{up} and the level of the diffuse emission $F^{(s)}$ at the cluster locations. The upper limit flux is computed according to $F^{\text{up}} = F^{(u)} + 2\sigma_{F^{(s)}}$, where $\sigma_{F^{(s)}}$ is the uncertainty of the total diffuse flux $F^{(s)}$.¹² This is the largest possible flux hidden under the diffuse γ -ray emission.

We find upper limit fluxes between $10^{-11} \text{ cm}^{-2} \text{ s}^{-1}$ and $10^{-8} \text{ cm}^{-2} \text{ s}^{-1}$ for the energy range 1–100 GeV. Ackermann et al. (2010, 2014a) provide upper limits for nearby clusters above 0.1 GeV. Some clusters are in both samples, e.g., A2256, A2319, *Coma* (A1656), *Ophiuchus*, *Perseus* (A0426), A1914, A2029, A2142, A2163, A2744, *Bullet* (1E 0657-56), MACSJ0717.5+3745. We find comparable or slightly lower upper limit fluxes. For example, for the *Coma* (A1656) cluster Ackermann et al. (2014a) report about $1.13 \times 10^{-10} \text{ cm}^{-2} \text{ s}^{-1}$ above 1 GeV, which is comparable to the $1.1 \times 10^{-10} \text{ cm}^{-2} \text{ s}^{-1}$ we obtain. However, we caution that our upper limits are not strict 95% confidence intervals, as they are not a direct outcome of our inference, but estimated as described above. A closer investigation is left for future work.

At the location of a few clusters in our sample we found a source in our point-source catalog. We marked these clusters in bold in Table 4 and reported the flux instead of an upper limit. Some of them are in projection to known γ -ray point-sources (active galaxies). These are, e.g., *Perseus* (NGC 1275 and IC310), A2390, and Virgo. Others are already present either in the second or in the third *Fermi* LAT source catalog, while ten are new detections (clusters marked with the symbol †). Noteworthy among the new detections are Hydra-A, and seven clusters hosting large-scale diffuse synchrotron emission. These are: A209, A2254, and RXCJ1514.9-1523 (radio halo), A2029, A2626, and RXJ1347.5-1145 (radio mini-halo), and A4038 (radio relic). An analysis at higher resolution is necessary to localize and better understand the origin of this emission.

4. Conclusions and summary

We analyze the *Fermi* LAT 6.5 year photon data in the energy range from 0.6 to 307.2 GeV. Applying the D³PO inference algorithm, the data are effectively denoised, deconvolved, and decomposed with Bayesian inference methods. In contrast to previous approaches by the *Fermi* collaboration and others, our non-parametric reconstruction does not rely on emission templates.

We obtain estimates for the diffuse and point-like contributions to the γ -ray flux. Furthermore, D³PO also provides uncertainty information and the *a priori* unknown angular power spectrum of the diffuse contribution.

The inferred diffuse photon flux reveals the diversity of the γ -ray sky. We clearly reproduce the structure of the Galactic disk, bulge, and local interstellar gas, all of which are primarily illuminated by photons induced by hadronic interactions of CRs with the ISM. We confirm the existence of the *Giant Fermi Bubbles*, as well as their homogeneous

¹² Unfortunately, D³PO does not converge on an all-sky point-like uncertainty map. When convergence is not achieved, a relative error of 1. is reported, see the uncertainty files available online.

Table 4. Overview of total flux upper limits for clusters hosting a radio (mini-)halo from the collection by Feretti et al. (2012). Clusters reported by Ackermann et al. (2010, 2014a) are also listed. For γ -ray detected clusters we give the actual flux estimates and mark those in bold. The symbol \dagger marks clusters present in our point source catalog for which an association with known sources is not yet available.

cluster name	$F_{\text{up}/\text{obs}}[\text{cm}^{-2}\text{s}^{-1}]$	$F^{(s)}[\text{cm}^{-2}\text{s}^{-1}]$
A85	8.5×10^{-11}	8.4×10^{-11}
A119	9.0×10^{-11}	8.2×10^{-11}
A133	5.4×10^{-11}	6.2×10^{-11}
A209 \dagger	7.6×10^{-11}	6.3×10^{-11}
A262	9.8×10^{-11}	1.2×10^{-10}
A399	8.7×10^{-11}	1.6×10^{-10}
A400	4.2×10^{-10}	1.7×10^{-10}
A401	1.2×10^{-10}	1.6×10^{-10}
A426	3.1×10^{-08}	2.6×10^{-10}
A478 \dagger	3.1×10^{-10}	2.8×10^{-10}
A496	7.6×10^{-11}	1.2×10^{-10}
A520	8.6×10^{-11}	1.2×10^{-10}
A521	9.1×10^{-11}	1.2×10^{-10}
A523	9.1×10^{-11}	1.8×10^{-10}
A545	2.1×10^{-10}	1.9×10^{-10}
A548e	5.9×10^{-11}	7.9×10^{-11}
A576	1.0×10^{-10}	1.2×10^{-10}
A665	5.7×10^{-11}	1.1×10^{-10}
A697	5.4×10^{-11}	8.8×10^{-11}
A746	4.5×10^{-11}	7.5×10^{-11}
A754	1.5×10^{-10}	1.0×10^{-10}
A773	7.7×10^{-11}	7.5×10^{-11}
A781	5.7×10^{-11}	7.8×10^{-11}
A851	4.7×10^{-11}	7.1×10^{-11}
A1060	1.4×10^{-10}	1.3×10^{-10}
A1213	7.6×10^{-11}	7.7×10^{-11}
A1300	2.2×10^{-10}	1.3×10^{-10}
A1351	5.1×10^{-11}	7.3×10^{-11}
A1367	6.7×10^{-11}	8.6×10^{-11}
A1644	1.0×10^{-10}	1.4×10^{-10}
A1656	1.1×10^{-10}	7.2×10^{-11}
A1689	8.2×10^{-11}	9.8×10^{-11}
A1758a	1.2×10^{-10}	6.9×10^{-11}
A1795	7.6×10^{-11}	6.7×10^{-11}
A1835	6.3×10^{-11}	1.0×10^{-10}
A1914	1.1×10^{-10}	8.1×10^{-11}
A1995	5.7×10^{-11}	6.8×10^{-11}
A2029 \dagger	2.2×10^{-10}	1.5×10^{-10}
A2034	5.2×10^{-11}	7.5×10^{-11}
A2065	9.0×10^{-11}	1.0×10^{-10}
A2142	6.2×10^{-11}	1.1×10^{-10}
A2163	2.6×10^{-10}	3.0×10^{-10}
A2199	7.3×10^{-11}	9.2×10^{-11}
A2218	5.9×10^{-11}	8.6×10^{-11}
A2219	1.1×10^{-10}	8.2×10^{-11}
A2244	6.0×10^{-11}	8.4×10^{-11}
A2254 \dagger	7.2×10^{-11}	1.5×10^{-10}
A2255	1.2×10^{-10}	8.9×10^{-11}
A2256	6.8×10^{-11}	1.0×10^{-10}
A2294	8.6×10^{-11}	1.5×10^{-10}
A2319	1.3×10^{-10}	1.7×10^{-10}
A2390	5.3×10^{-11}	1.6×10^{-10}
A2589	1.1×10^{-10}	1.1×10^{-10}
A2597	5.1×10^{-11}	6.6×10^{-11}
A2626 \dagger	7.2×10^{-11}	1.2×10^{-10}
A2634	7.6×10^{-11}	1.1×10^{-10}
A2657	1.1×10^{-10}	1.2×10^{-10}
A2734	5.7×10^{-11}	6.3×10^{-11}
A2744	8.2×10^{-11}	6.3×10^{-11}

morphology, sharp edges, and hard spectra. Moreover, we are also able to resolve small diffuse structures; e.g., the γ -ray glow around *Centaurus A*.

cluster name	$F_{\text{up}/\text{obs}}[\text{cm}^{-2}\text{s}^{-1}]$	$F^{(s)}[\text{cm}^{-2}\text{s}^{-1}]$
A2877	4.2×10^{-11}	5.6×10^{-11}
A3112	4.1×10^{-11}	6.2×10^{-11}
A3158	5.2×10^{-11}	6.6×10^{-11}
A3266	8.9×10^{-11}	8.3×10^{-11}
A3376	2.3×10^{-10}	1.3×10^{-10}
A3526	1.5×10^{-10}	2.1×10^{-10}
A3562	9.5×10^{-11}	1.6×10^{-10}
A3571	1.1×10^{-10}	1.7×10^{-10}
A3627	2.1×10^{-10}	4.7×10^{-10}
A3822	8.9×10^{-11}	8.9×10^{-11}
A3827	6.4×10^{-11}	8.4×10^{-11}
A3921 \dagger	1.2×10^{-11}	7.7×10^{-11}
A4038 \dagger	1.6×10^{-11}	6.8×10^{-11}
A4059	8.5×10^{-11}	5.6×10^{-11}
1E0657-56	7.6×10^{-11}	1.5×10^{-10}
2A0335+096	1.9×10^{-10}	2.7×10^{-10}
3C129	3.7×10^{-10}	8.6×10^{-10}
AWM7	1.2×10^{-10}	1.7×10^{-10}
CIZA J2242.8+5301	2.8×10^{-10}	3.7×10^{-10}
CL0016+16	6.5×10^{-11}	1.1×10^{-10}
CL0217+70	2.6×10^{-10}	5.7×10^{-10}
EXO0422-086	1.4×10^{-10}	1.3×10^{-10}
FORNAX	6.7×10^{-11}	6.8×10^{-11}
HCG94	1.6×10^{-10}	1.4×10^{-10}
HYDRA-A \dagger	3.4×10^{-11}	9.5×10^{-11}
IIZw54	1.1×10^{-10}	2.3×10^{-10}
IIZw108	8.1×10^{-11}	1.2×10^{-10}
M49	6.0×10^{-11}	9.2×10^{-11}
MACSJ0717.5+3745	1.2×10^{-10}	1.2×10^{-10}
MRC0116+111	7.6×10^{-11}	9.6×10^{-11}
NGC1550	1.0×10^{-10}	2.0×10^{-10}
NGC5044	1.1×10^{-10}	1.4×10^{-10}
NGC4636	7.3×10^{-11}	1.0×10^{-10}
NGC5813	1.2×10^{-10}	1.5×10^{-10}
NGC5846	1.4×10^{-10}	1.7×10^{-10}
Ophiuchus	2.9×10^{-10}	7.0×10^{-10}
RBS797	6.5×10^{-11}	7.5×10^{-11}
RXJ0107.7+5408	1.5×10^{-10}	3.4×10^{-10}
RXCJ1314.4-2515	9.6×10^{-11}	1.9×10^{-10}
RXCJ1514.9-1523 \dagger	4.0×10^{-11}	2.0×10^{-10}
RXCJ2003.5-2323	3.5×10^{-10}	2.1×10^{-10}
RXJ1347.5-1145 \dagger	5.5×10^{-11}	1.5×10^{-10}
RXCJ1504.1-0248	1.9×10^{-10}	2.0×10^{-10}
RXCJ2344.2-0422	7.1×10^{-11}	9.0×10^{-11}
S405	6.9×10^{-11}	1.3×10^{-10}
S540	5.7×10^{-11}	9.9×10^{-11}
S636	1.2×10^{-10}	1.5×10^{-10}
TRIANGULUM	1.2×10^{-10}	2.9×10^{-10}
UGC03957	2.0×10^{-10}	1.2×10^{-10}
VIRGO	1.2×10^{-09}	1.1×10^{-10}
ZwCl1742.1+3306	1.5×10^{-09}	1.2×10^{-10}

The continuous reconstruction of the diffuse flux allows us to present the first spectral index map of the diffuse γ -ray sky, as well as a pseudocolor composite visualizing the spectrally different regions. Furthermore, the large-scale angular power spectrum of the diffuse emission seems to obey a power-law with index 2.47 ± 0.02 across all energy bands.

Inspired by the pseudocolor visualization, we decompose the diffuse γ -ray sky into a “cloud”-like and “bubble”-like emission component. The former, tracing the dense, cold ISM, is dominated by hadronic emission processes, while the latter, being morphologically and spectrally distinct, seems to be dominated by leptonic processes in hot, dilute parts of the ISM and outflows thereof. In particular, our findings indicate a preference for IC emission from the *Fermi* bubbles and support scenarios in which the *Fermi* bubbles are explained by hot outflows powered by strong

activities in the Galactic center region (Yang et al. 2013; Cheng et al. 2011; Dogiel et al. 2011; Chernyshov 2011; Carretti et al. 2013). We report further, smaller outflows of a similar population of relativistic particles at other locations.

The reconstruction of the point-like photon flux qualitatively confirms most of the sources from the second and third *Fermi* LAT source catalog. Quantitatively, we derive the first D³PO *Fermi* catalog of γ -ray source candidates that comprises 3,106 point sources. A more detailed analysis of this catalog is left for future research.

Finally, we observe γ -ray emission in the direction of a few galaxy clusters hosting known radio halos. Further analysis is required to shed light on the origin of this emission.

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Some of the results in this publication have been derived using NUMPY/SCIPY (Oliphant 2006), MATPLOTLIB (Hunter 2007), HEALPIX (Górski et al. 2005), and especially the D³PO algorithm (Selig & Enßlin 2013) based on the NIFTY package (Selig et al. 2013).

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References

- Abdo, A. A., Ackermann, M., Ajello, M., et al., Fermi Large Area Telescope First Source Catalog, *ApJS* **188** (Jun. 2010) 405–436, [arXiv:1002.2280 \[astro-ph.HE\]](#)
- Abdo, A. A., Ackermann, M., Ajello, M., et al., The on-orbit calibration of the Fermi Large Area Telescope, *Astroparticle Physics* **32** (Oct. 2009) 193–219, [arXiv:0904.2226 \[astro-ph.IM\]](#)
- Abdo, A. A., Ackermann, M., Ajello, M., et al., Spectrum of the Isotropic Diffuse Gamma-Ray Emission Derived from First-Year Fermi Large Area Telescope Data, *Physical Review Letters* **104** no. 10, (Mar. 2010) 101101, [arXiv:1002.3603 \[astro-ph.HE\]](#)
- Ackermann, M., Ajello, M., Albert, A., et al., The Fermi Large Area Telescope on Orbit: Event Classification, Instrument Response Functions, and Calibration, *ApJS* **203** (Nov. 2012) 4, [arXiv:1206.1896 \[astro-ph.IM\]](#)
- Ackermann, M., Ajello, M., Albert, A., et al., Search for Cosmic-Ray-induced Gamma-Ray Emission in Galaxy Clusters, *ApJ* **787** (May 2014) 18, [arXiv:1308.5654 \[astro-ph.HE\]](#)
- Ackermann, M., Ajello, M., Albert, A., Atwood, W. B., & Fermi LAT Collaboration, The spectrum of isotropic diffuse gamma-ray emission between 100 MeV and 820 GeV, *ArXiv e-prints* (Oct. 2014), [arXiv:1410.3696 \[astro-ph.HE\]](#)
- Ackermann, M., Ajello, M., Albert, A., et al., Fermi LAT search for dark matter in gamma-ray lines and the inclusive photon spectrum, *Phys. Rev. D* **86** no. 2, (Jul. 2012) 022002, [arXiv:1205.2739 \[astro-ph.HE\]](#)
- Ackermann, M., Ajello, M., Allafort, A., et al., In-flight measurement of the absolute energy scale of the Fermi Large Area Telescope, *Astroparticle Physics* **35** (Jan. 2012) 346–353, [arXiv:1108.0201 \[astro-ph.IM\]](#)
- Ackermann, M., Ajello, M., Allafort, A., et al., GeV Gamma-ray Flux Upper Limits from Clusters of Galaxies, *ApJ* **717** (Jul. 2010) L71–L78, [arXiv:1006.0748 \[astro-ph.HE\]](#)
- Ackermann, M., Ajello, M., Atwood, W. B., et al., Fermi-LAT Observations of the Diffuse Gamma-Ray Emission: Implications for Cosmic Rays and the Interstellar Medium, *ArXiv e-prints* (Feb. 2012), [arXiv:1202.4039 \[astro-ph.HE\]](#)
- Ackermann, M., Albert, A., Atwood, W. B., & Fermi LAT Collaboration, The Spectrum and Morphology of the Fermi Bubbles, *ArXiv e-prints* (Jul. 2014), [arXiv:1407.7905 \[astro-ph.HE\]](#)
- Ackermann, M., Jóhannesson, G., Digel, S., et al., A method to analyze the diffuse gamma-ray emission with the Fermi Large Area Telescope, in *American Institute of Physics Conference Series*, Vol. 1085, American Institute of Physics Conference Series, ed. F. A. Aharonian, W. Hofmann, & F. Rieger. 2008, 763–766
- Atwood, W. B., Abdo, A. A., Ackermann, M., et al., The Large Area Telescope on the Fermi Gamma-Ray Space Telescope Mission, *ApJ* **697** (Jun. 2009) 1071–1102, [arXiv:0902.1089 \[astro-ph.IM\]](#)
- Bayes, T., An Essay towards Solving a Problem in the Doctrine of Chances, *Philosophical Transactions of the Royal Society* **35** (1763) 370–418, <http://journals.royalsociety.org/content/w24177406t384j06/>
- Brageon, J., Charles, E., & M. Wood for the Fermi-LAT collaboration, Fermi-LAT data reprocessed with updated calibration constants, *ArXiv e-prints* (Apr. 2013), [arXiv:1304.5456 \[astro-ph.HE\]](#)
- Carretti, E., Crocker, R. M., Staveley-Smith, L., et al., Giant magnetized outflows from the centre of the Milky Way, *Nature* **493** (Jan. 2013) 66–69, [arXiv:1301.0512 \[astro-ph.GA\]](#)
- Cheng, K.-S., Chernyshov, D. O., Dogiel, V. A., Ko, C.-M., & Ip, W.-H., Origin of the Fermi Bubble, *ApJ* **731** (Apr. 2011) L17, [arXiv:1103.1002 \[astro-ph.HE\]](#)
- Chernyshov, D., Particle acceleration and the origin of gamma-ray emission from Fermi Bubbles, *International Cosmic Ray Conference* **7** (2011) 11–18, [arXiv:1109.2619 \[astro-ph.GA\]](#)
- Conrad, J., Searches for particle dark matter with gamma-rays, in *American Institute of Physics Conference Series*, Vol. 1505, American Institute of Physics Conference Series, ed. F. A. Aharonian, W. Hofmann, & F. M. Rieger. 2012, 166–176, [arXiv:1210.4392 \[astro-ph.CO\]](#)
- Cox, R. T., Probability, Frequency and Reasonable Expectation, *American Journal of Physics* **14** (Jan. 1946) 1
- Crocker, R. M. & Aharonian, F., Fermi Bubbles: Giant, Multibillion-Year-Old Reservoirs of Galactic Center Cosmic Rays, *Phys. Rev. Lett.* **106** (Mar 2011) 101102, <http://link.aps.org/doi/10.1103/PhysRevLett.106.101102>
- de Boer, W. & Weber, M., Fermi Bubbles and Bubble-like Emission from the Galactic Plane, *ApJ* **794** (Oct. 2014) L17, [arXiv:1407.4114 \[astro-ph.HE\]](#)
- Dermer, C. D., The Extragalactic γ Ray Background, in *American Institute of Physics Conference Series*, Vol. 921, The First GLAST Symposium, ed. S. Ritz, P. Michelson, & C. A. Meegan. 2007, 122–126, [arXiv:0704.2888](#)
- Dermer, C. D., Strong, A. W., Orlando, E., Tibaldo, L., & for the Fermi Collaboration, Determining the Spectrum of Cosmic Rays in Interstellar Space from the Diffuse Galactic Gamma-Ray Emission, *ArXiv e-prints* (Jul. 2013), [arXiv:1307.0497 \[astro-ph.HE\]](#)
- Dogiel, V. A., Chernyshov, D. O., Cheng, K., et al., Fermi Bubbles as a Result of Star Capture in the Galactic Center, *ArXiv e-prints* (Sep. 2011), [arXiv:1109.6087 \[astro-ph.HE\]](#)
- Enßlin, T., Information field theory, in *American Institute of Physics Conference Series*, Vol. 1553, American Institute of Physics Conference Series, ed. U. von Toussaint. 2013, 184–191, [arXiv:1301.2556 \[astro-ph.IM\]](#)
- Enßlin, T., Astrophysical data analysis with information field theory, in *American Institute of Physics Conference Series*, American Institute of Physics Conference Series. 2014, [arXiv:1405.7701 \[astro-ph.IM\]](#)
- Enßlin, T. A. & Frommert, M., Reconstruction of signals with unknown spectra in information field theory with parameter uncertainty, *Phys. Rev. D* **83** no. 10, (May 2011) 105014–+, [arXiv:1002.2928 \[astro-ph.IM\]](#)

- Enßlin, T. A., Frommert, M., & Kitaura, F. S., Information field theory for cosmological perturbation reconstruction and nonlinear signal analysis, *Phys. Rev. D* **80** no. 10, (Nov. 2009) 105005–+, [arXiv:0806.3474](#)
- Feretti, L., Giovannini, G., Govoni, F., & Murgia, M., Clusters of galaxies: observational properties of the diffuse radio emission, *A&A Rev.* **20** (May 2012) 54, [arXiv:1205.1919](#) [[astro-ph.CO](#)]
- Finkbeiner, D. P., Davis, M., & Schlegel, D. J., Extrapolation of Galactic Dust Emission at 100 Microns to Cosmic Microwave Background Radiation Frequencies Using FIRAS, *ApJ* **524** (Oct. 1999) 867–886, [astro-ph/9905128](#)
- Górski, K. M., Hivon, E., Banday, A. J., et al., HEALPix: A Framework for High-Resolution Discretization and Fast Analysis of Data Distributed on the Sphere, *ApJ* **622** (Apr. 2005) 759–771, [arXiv:astro-ph/0409513](#)
- Greiner, M. & Enßlin, T. A., Conversion between the power spectra of a field and its logarithm, *ArXiv e-prints* (Dec. 2013), [arXiv:1312.1354](#) [[astro-ph.CO](#)]
- Guglielmetti, F., Fischer, R., & Dose, V., Background-source separation in astronomical images with Bayesian probability theory - I. The method, *MNRAS* **396** (Jun. 2009) 165–190, [arXiv:0903.2342](#) [[astro-ph.IM](#)]
- Haslam, C. G. T., Salter, C. J., Stoffel, H., & Wilson, W. E., A 408 MHz all-sky continuum survey. II - The atlas of contour maps, *A&AS* **47** (Jan. 1982) 1, *ADS*
- Hunter, J. D., *Matplotlib: A 2D graphics environment*, *Computing In Science & Engineering* **9** no. 3, (2007) 90–95
- Jasche, J., Kitaura, F. S., Wandelt, B. D., & Enßlin, T. A., Bayesian power-spectrum inference for large-scale structure data, *MNRAS* **406** (Jul. 2010) 60–85, [arXiv:0911.2493](#) [[astro-ph.CO](#)]
- Jasche, J. & Wandelt, B. D., Methods for Bayesian Power Spectrum Inference with Galaxy Surveys, *ApJ* **779** (Dec. 2013) 15, [arXiv:1306.1821](#) [[astro-ph.CO](#)]
- Johannesson, G., Orlando, E., & for the Fermi-LAT collaboration, Accounting for the Sun and the Moon in Fermi-LAT Analysis, *ArXiv e-prints* (Jun. 2013), [arXiv:1307.0197](#) [[astro-ph.IM](#)]
- Large, M. I., Quigley, M. J. S., & Haslam, C. G. T., A new feature of the radio sky, *MNRAS* **124** (1962) 405
- Moskalenko, I. V. & Strong, A. W., Anisotropic Inverse Compton Scattering in the Galaxy, *ApJ* **528** (Jan. 2000) 357–367, [astro-ph/9811284](#)
- Nolan, P. L., Abdo, A. A., Ackermann, M., et al., Fermi Large Area Telescope Second Source Catalog, *ApJS* **199** (Apr. 2012) 31, [arXiv:1108.1435](#) [[astro-ph.HE](#)]
- Oliphant, T. 2006, *A Guide to NumPy*, Trelgol Publishing
- Oppermann, N., Selig, M., Bell, M. R., & Enßlin, T. A., Reconstruction of Gaussian and log-normal fields with spectral smoothness, [arXiv:1210.6866](#) [[astro-ph.IM](#)]
- Planck Collaboration, Planck 2013 results. XI. All-sky model of thermal dust emission, *ArXiv e-prints* (Dec. 2013), [arXiv:1312.1300](#)
- Planck Collaboration, Planck intermediate results. IX. Detection of the Galactic haze with Planck, *A&A* **554** (Jun. 2013) A139, [arXiv:1208.5483](#) [[astro-ph.GA](#)]
- Planck Collaboration, Planck intermediate results. XXVIII. Interstellar gas and dust in the Chamaeleon clouds as seen by Fermi LAT and Planck, *ArXiv e-prints* (Sep. 2014), [arXiv:1409.3268](#) [[astro-ph.HE](#)]
- Portillo, S. K. N. & Finkbeiner, D. P., Sharper Fermi LAT Images: instrument response functions for an improved event selection, *ArXiv e-prints* (Jun. 2014), [arXiv:1406.0507](#) [[astro-ph.IM](#)]
- Schmitt, J., Starck, J. L., Casandjian, J. M., Fadili, J., & Grenier, I., Poisson denoising on the sphere: application to the Fermi gamma ray space telescope, *A&A* **517** (Jul. 2010) A26, [arXiv:1003.5613](#) [[astro-ph.IM](#)]
- Schmitt, J., Starck, J. L., Casandjian, J. M., Fadili, J., & Grenier, I., Multichannel Poisson denoising and deconvolution on the sphere: application to the Fermi Gamma-ray Space Telescope, *A&A* **546** (Oct. 2012) A114, [arXiv:1206.2787](#) [[astro-ph.IM](#)]
- Selig, M., Bell, M. R., Junklewitz, H., et al., NIFTY - Numerical Information Field Theory - a versatile Python library for signal inference, *A&A* **554** (Apr. 2013) A26, [arXiv:1301.4499](#) [[astro-ph.IM](#)]
- Selig, M. & Enßlin, T. A., Denoising, Deconvolving, and Decomposing Photon Observations, [arXiv:1311.1888](#) [[astro-ph.IM](#)]
- Shannon, C. E., A mathematical theory of communication, *Bell System Technical Journal* **27** (1948) 379–423
- Sreekumar, P., Bertsch, D. L., Dingus, B. L., et al., EGRET Observations of the Extragalactic Gamma-Ray Emission, *ApJ* **494** (Feb. 1998) 523–534, [astro-ph/9709257](#)
- Strong, A. W., Moskalenko, I. V., & Reimer, O., Diffuse Continuum Gamma Rays from the Galaxy, *ApJ* **537** (Jul. 2000) 763–784, [astro-ph/9811296](#)
- Su, M. & Finkbeiner, D. P., Evidence for Gamma-Ray Jets in the Milky Way, *ApJ* **753** (Jul. 2012) 61, [arXiv:1205.5852](#) [[astro-ph.HE](#)]
- Su, M., Slatyer, T. R., & Finkbeiner, D. P., Giant Gamma-ray Bubbles from Fermi-LAT: Active Galactic Nucleus Activity or Bipolar Galactic Wind?, *ApJ* **724** (Dec. 2010) 1044–1082, [arXiv:1005.5480](#) [[astro-ph.HE](#)]
- The Fermi-LAT Collaboration, Fermi Large Area Telescope Third Source Catalog, *ArXiv e-prints* (Jan. 2015), [arXiv:1501.02003](#) [[astro-ph.HE](#)]
- Wandelt, B. D., Larson, D. L., & Lakshminarayanan, A., Global, exact cosmic microwave background data analysis using Gibbs sampling, *Phys. Rev. D* **70** no. 8, (Oct. 2004) 083511, [arXiv:astro-ph/0310080](#)
- Wiener, N. 1949, *Extrapolation, Interpolation and Smoothing of Stationary Time Series, with Engineering Applications*, Technology Press and Wiley, New York, note: Originally issued in Feb 1942 as a classified Nat. Defense Res. Council Rep.
- Yang, H.-Y. K., Ruzkowski, M., & Zweibel, E., The Fermi bubbles: gamma-ray, microwave and polarization signatures of leptonic AGN jets, *MNRAS* **436** (Dec. 2013) 2734–2746, [arXiv:1307.3551](#) [[astro-ph.GA](#)]
- Yang, R.-z., Aharonian, F., & Crocker, R., The Fermi bubbles revisited, *A&A* **567** (Jul. 2014) A19, [arXiv:1402.0403](#) [[astro-ph.HE](#)]

Appendix A: Data analysis

Appendix A.1: Data selection

In this work, we analyze the 6.5 years of observational data taken by the *Fermi* LAT; i.e., data from mission weeks 9 to 346 (mission elapsed time 239,557,417 s to 443,556,512 s). The data are subject to multiple restrictions and cuts detailed in the following.

For our analysis we exclusively consider events classified as P7REP_CLEAN_V15 in the reprocessed Pass 7 data set. The CLEAN events, which are “cleaned” of CR interactions with the instrument, are recommended for studies of the diffuse γ -ray emission.¹³ Events with rocking angles (between the LAT boresight and zenith) above 52° and zenith angles above 100° are excluded in order to suppress contaminations from CRs and the Earth’s limb (Atwood et al. 2009).¹⁴ In addition, we apply a (non-standard) cut with respect to the angular distance to the Sun that we require to exceed 20° . This way, almost all Solar γ -rays are rejected at the price of reducing the total number of events by less than 3%. A similar procedure regarding the moon is conceivable but ignored, because its contribution is negligible.

The individual events are labeled FRONT or BACK according to whether the photon has been converted in the front or back section of the LAT instrument. We retain this labeling, but combine those data vectors by a direct sum; i.e.,

$$\mathbf{d} = \mathbf{d}^{\text{FRONT}} \oplus \mathbf{d}^{\text{BACK}} = (\mathbf{d}^{\text{FRONT}}, \mathbf{d}^{\text{BACK}})^\top. \quad (\text{A.1})$$

The selected events are binned in nine (logarithmically equally spaced) energy bins ranging from 0.6 to 307.2 GeV, cf. Table 1. We also apply a spatial binning of the events into all-sky count maps using a HEALPIX discretization with $n_{\text{side}} = 128$, which corresponds to 196,608 pixels with a size of roughly $64 \mu\text{sr} \approx (0.46^\circ)^2$ each.

¹³ For further details regarding the *Fermi* LAT data products see <http://fermi.gsfc.nasa.gov/ssc/data/>.

¹⁴ The exact filter expression reads “DATA_QUAL>0 && LAT_CONFIG==1 && ABS(ROCK_ANGLE)<52 && ZENITH<100”.

For a proper deconvolution, our analysis has to take the LAT’s PSF and exposure into account. The instrumental response functions of the *Fermi* LAT (Atwood et al. 2009; Abdo et al. 2009; Ackermann et al. 2012a), which are essential therefor, have been improved in the reprocessed Pass 7 release, and are available within the *Fermi* Science Tools. According to our event selection, we make use of the P7REP_CLEAN_V15::FRONT and BACK IRFs, respectively. These can be assumed to be accurately calibrated, although further improvements, especially at low energies, are under discussion (Portillo & Finkbeiner 2014). Given the IRFs, the exposure ($\varepsilon_{ij}^{\text{FRONT}}, \varepsilon_{ij}^{\text{BACK}}$) for each HEALPIX pixel i and each energy band j can be retrieved from the data archive. In order to compute ε , the Sun exposure is subtracted from the “standard” exposure due to the chosen rejection of potential Solar events (Johannesson et al. 2013). The PSF of the *Fermi* LAT is a function of position and energy E . Its shape varies slightly with spatial translation and sharpens strongly with increasing energy. The forward application of the PSF is a linear operation that can be implemented in form of a convolution matrix evaluating the PSF at each pixel center and for each energy band. This matrix is fairly sparse because of the vanishing tails of the PSF, and is computed beforehand. The exposure and the PSF define the instrument response operator \mathbf{R} ,

$$R_{ij}(x) \propto \frac{1}{(E_j^{\text{max}} - E_j^{\text{min}})} \begin{pmatrix} \varepsilon_{ij}^{\text{FRONT}} \times \text{PSF}_i^{\text{FRONT}}(E_j^{\text{mid}}, x) \\ \varepsilon_{ij}^{\text{BACK}} \times \text{PSF}_i^{\text{BACK}}(E_j^{\text{mid}}, x) \end{pmatrix}, \quad (\text{A.2})$$

up to a proportionality constant that can absorb numerical factors and physical units. Notice that this definition does not include a spectral convolution; i.e., no cross-talk between different energy bands is assumed.

The primary target of our analysis is the physical photon flux $\phi = \phi(x)$, which is a function of position $x \in \Omega$. Here, the position space Ω is the observational sphere, and the position x might be given in spherical coordinates (φ, θ) , or in Galactic longitude and latitude (l, b) .

The response operator \mathbf{R} describes the mapping of a photon flux ϕ to $\lambda = \mathbf{R}\phi$ by a convolution with the IRFs; i.e.,

$$\lambda_{ij} = \int_{\Omega} dx R_{ij}(x) \phi(x), \quad (\text{A.3})$$

where λ describes the noiseless (non-integer) number of photons one expects to observe through the IRFs given some photon flux in the sky. This expected number of counts λ relates to the observed (integer) photon counts \mathbf{d} by a noise process, which is part of the statistical model detailed in the next section.

Appendix A.2: Inference algorithm

The foundation of the analysis presented in this work is the D³PO inference algorithm derived by Selig & Enßlin (2013) that targets the denoising, deconvolution and decomposition of photon observations. Without going into technical details, we briefly review the underlying assumptions and characteristics of the D³PO algorithm in the following.

The observed photon count data \mathbf{d} carries information about the astrophysical photon flux ϕ , as well as noise and instrumental imprints. In order to optimally reconstruct ϕ

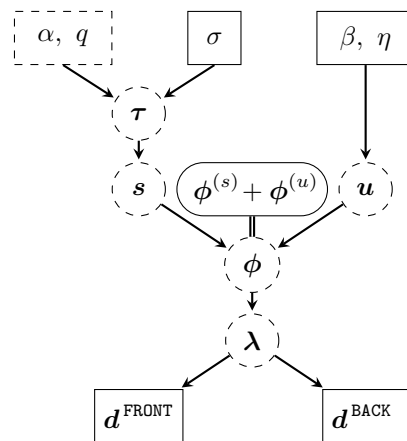


Fig. A.1. Graphical model of the model parameters α , q , σ , β , and η , the logarithmic angular power spectrum τ , the diffuse and point-like signal fields, \mathbf{s} and \mathbf{u} , the photon fluxes, ϕ , $\phi^{(s)}$, and $\phi^{(u)}$, and the expected and observed number of photons, λ and \mathbf{d} .

given \mathbf{d} , we incorporate our knowledge about the actual measurement in a data model that consists of deterministic relations and probabilistic processes. Hence, D³PO is a probabilistic algorithm conducting Bayesian inference.

We can assume the photon counts to suffer from Poissonian shot noise; i.e., the data entries d_{ij} are the outcomes of statistically independent Poisson processes given an expected number of counts λ_{ij} each. Especially in low photon flux regions and at high energies, where the signal-to-noise ratios are worst, using a Poissonian likelihood allows for an accurate noise treatment whereas Gaussian noise approximations often fail.

D³PO’s deconvolution task covers the correction of all effects that trace back to the instrumental response \mathbf{R} . As discussed in Section A.1, this response establishes a relation between the astrophysical photon flux ϕ and the expected counts λ by taking the IRFs of the *Fermi* LAT fully into account. Since we suppose the IRFs to be thoroughly calibrated (to the best of our knowledge), this relation is deterministic.

The total photon flux ϕ consists of many different contributions that can be divided into two morphological classes, diffuse and point-like contributions. Diffuse emission, which is produced by the interaction of CRs with the ISM, unresolved point sources and extragalactic background, is characterized by spatially smooth fluctuations. On the contrary, point-like emission is fairly local originating primarily from resolved point sources. The D³PO algorithm reconstructs the total photon flux as the sum of a diffuse and point-like flux contribution; i.e.,

$$\phi = \phi^{(s)} + \phi^{(u)} = \phi_0 (e^{\mathbf{s}} + e^{\mathbf{u}}), \quad (\text{A.4})$$

where ϕ_0 is a constant absorbing numerical factors and flux units, and the exponentiation is applied pixelwise to the diffuse and point-like signal fields, \mathbf{s} and \mathbf{u} . Those signal fields describe the dimensionless logarithmic flux ensuring the positivity of the physical photon flux in a natural way. Although the algorithm deals with the \mathbf{s} and \mathbf{u} fields for numerical reasons, we only regard the fluxes $\phi^{(s)}$ and $\phi^{(u)}$ in the following as they are physical.

We can incorporate our naive understanding of “diffuse” and “point-like” by introducing prior assumptions. Embedding *a priori* knowledge on the solution, of course, biases the inference. However, priors also remedy the degeneracy of the inference problem as they suppress counterintuitive solutions.

The diffuse photon flux $\phi^{(s)}$, being spatially smooth, is expected to exhibit spatial correlation. Without enforcing concrete spatial features, such as a Galactic profile, we assume $\phi^{(s)}$ to obey multivariate log-normal statistics. Assuming, furthermore, statistical homogeneity and isotropy, the underlying covariance is determined by an *a priori* unknown angular power spectrum. In order to retain a flexible handle on this power spectrum, we further introduce hyperpriors (cf. e.g., Enßlin & Frommert 2011; Oppermann et al. 2012; Selig & Enßlin 2013). We assume a (asymptotically) uniform prior for the logarithmic angular power and a spectral smoothness prior as suggested by Oppermann et al. (2012). This introduces scalar model parameters α , q , and σ .

The point-like photon flux $\phi^{(u)}$ exhibits strong features that appear to be fairly rare and local. We assume $\phi^{(u)}$ to follow statistically independent inverse-Gamma distributions described by the model parameters β and η .

For a detailed derivation and discussion of the probabilistic model D³PO is based on, we refer to Selig & Enßlin (2013). An illustrative graphical model of the introduced hierarchy of Bayesian parameters is shown in Fig. A.1.

Appendix A.3: Analysis procedure

In theory, we could apply the D³PO algorithm to the whole data set at once. However, it is computationally more efficient to exploit the spectral separability of the response model by applying the algorithm to each energy band individually, cf. Eq. A.2. In order to exploit spectral correlations, we propose to align the priors of the diffuse component after an initial inference run by defining a common angular power spectrum. This yields a three-step analysis procedure detailed in the following.

Initial inference: The D³PO algorithm is applied to each energy band separately, which can be done in parallel.

We fix the model parameters with fairly soft constraints, by setting $\alpha = 1$, $q = 10^{-12}$, $\sigma = 10$, $\beta = \frac{3}{2}$, and $\eta = 10^{-2}$. The limit of $(\alpha, q) \rightarrow (1, 0)$ leads to uniform prior for the logarithmic angular power spectrum τ of the diffuse photon flux (Enßlin & Frommert 2011), but choosing a non-zero q is numerically more stable. The spectral smoothness parameter σ is the *a priori* standard deviation of the second derivative of $\tau = \tau_\ell$ with respect to the logarithm of the angular quantum number ℓ ; i.e., σ describes the tolerance of deviations from a power-law shape (Oppermann et al. 2012). The parameter tuple (β, η) determines the slope and scale of the inverse-Gamma prior of the point-like photon flux. While a slope of $\frac{3}{2}$ is generally applicable, the scale, for which we find 10^{-2} fitting, has to be adapted according to the chosen resolution (Selig & Enßlin 2013).

D³PO solves an inference problem that is non-linear and, in general, non-convex. To circumvent a dependence on its initialization, D³PO can generate suitable starting values by solving a coarse grained inference problem first.

For this purpose only, we provide a binary exposure masking the most prominent point sources.

Prior alignment: The prior of the diffuse component describes our *a priori* expectation of how spatially smooth the emission is. If we find diffuse structures of a certain size at one energy band, we can expect to find similar structures at neighboring bands, especially since most diffuse emission processes exhibit power-law-like energy spectra. Thus, we expect significant spectral correlations, in particular for prominent features such as the Galactic bulge, for example. Since the incorporation of a spectral convolution in the response is computationally infeasible, we impose an aligning of the diffuse priors to exploit spectral correlations, nonetheless.

The diffuse prior is defined by the logarithmic angular power spectrum τ . As discussed in Sec. 3.4, we find a rough power-law behavior of the power spectra with deviations due to the Galactic disk and finite exposure. Fig. 11 shows the results of the initial inference, in particular including a power spectrum fit averaged across the energy bands. This average spectrum defines the aligned prior. Notice that the apparent excess of small-scale power for high energy bands, comparing inferred and aligned power spectra, remedies potential perception thresholds occurring during the inference (Enßlin & Frommert 2011).

Afterwards, we also align the diffuse maps within the initially masked regions according to the aligned prior in order to avoid artifacts due to initialization.¹⁵

The alignment of the point-like priors, through β and η , has proven ineffective in tests and is therefore omitted.

Final inference: The D³PO algorithm is applied to each energy band separately, again. For this run, however, we keep the (aligned) angular power spectrum fixed and provide the aligned diffuse maps as starting values. Hence, the initially used binary mask is not required any more. Notice that a fixed angular power spectrum renders the model parameters α , q , and σ obsolete.

¹⁵ We minimize the prior term, $\mathbf{s}^\dagger \mathbf{S}^{-1} \mathbf{s}$, but only for $s(x|x = (\varphi, \theta) \in \text{mask} \wedge x \sim (\ell, m) \neq (2N, 0))$ ensuring the preservation of the Galactic profile and the reconstructed field values outside the mask.